

# Equivalent Correlation between Short Channel DG & GAA MOSFETs

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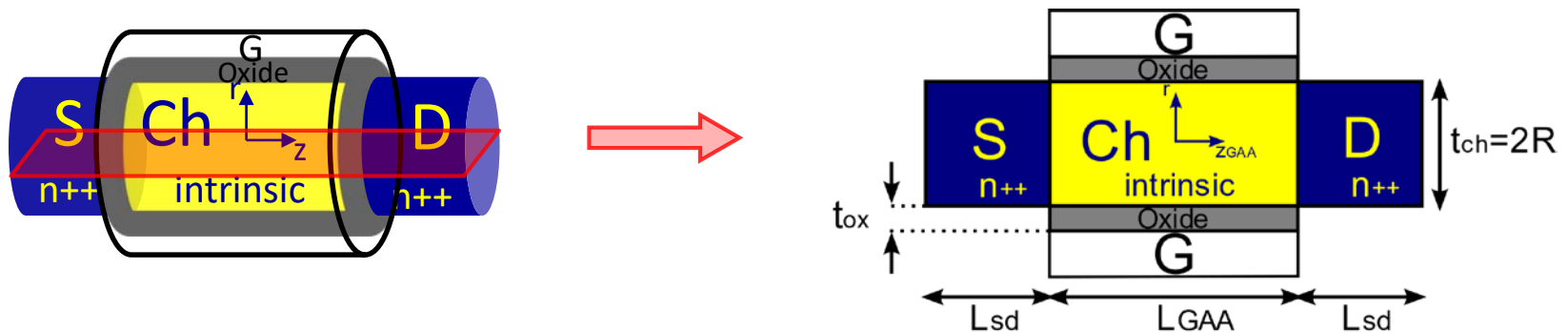
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MOS-AK at ESSDERC/ESSCIRC

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# Motivation

- Status quo: Concept of equivalent thickness and capacitance (long channel) [1].
- Goal: Extend 2-D DG compact model [2] to short channel GAA MOSFETs.
- Challenge: Stretch the channel length to equalize electrostatics & short channel behavior.
- Methods:
  1. Theory derived from the Laplace's & Poisson's equation.
  2. Concept of equivalent channel length due to equiv. capacitance.

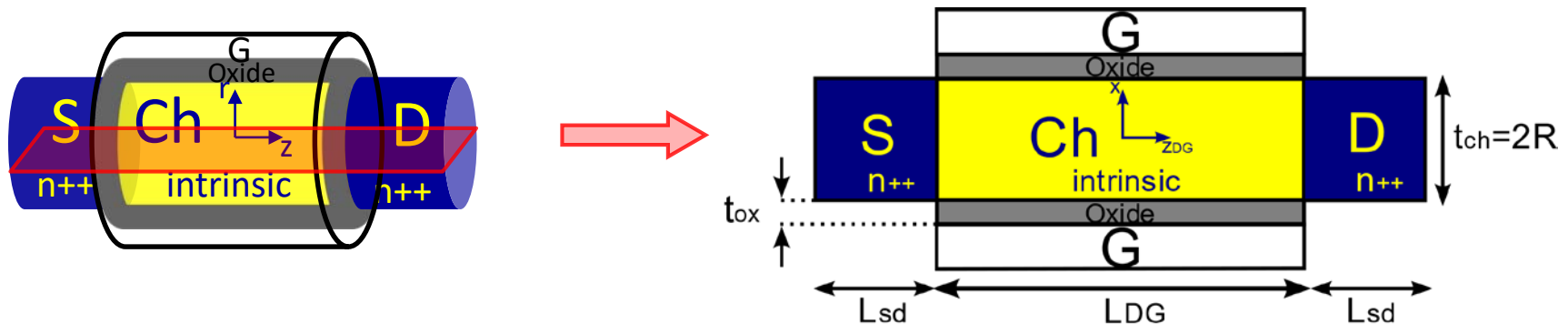


[1] N. Chevillon et al., IEEE TED, Vol. 59, no. 1, pp. 60-71, January 2012.

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# Outline

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1. Introduction
2. Device dimensions dependent equivalent length
3. Simulation & Compact Model Results
4. Conclusion

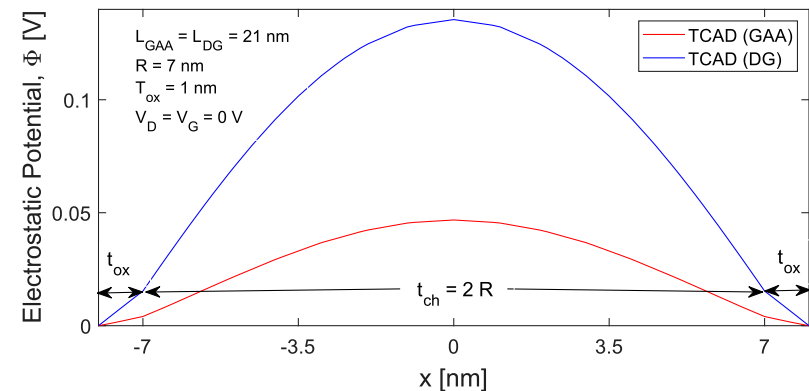
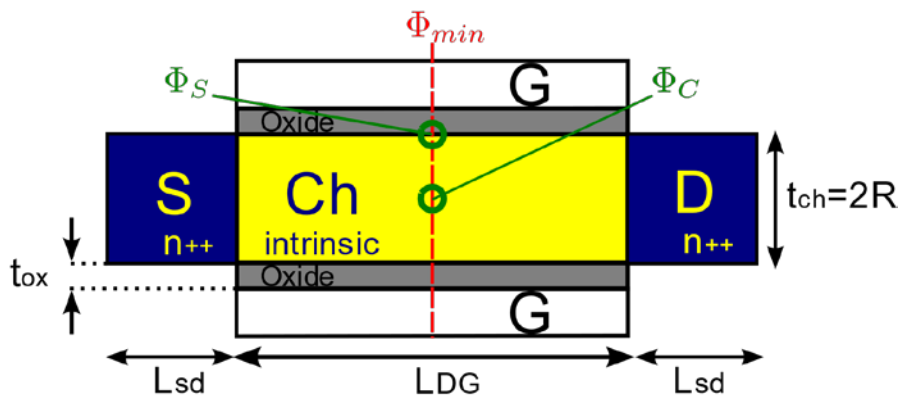
# 1. Introduction

## Subthreshold equivalent potential theory:

- Current model [3]:  $I_D \propto \int \frac{n_i^2}{N_A} e^{\Phi_{\min}/V_t} dx$
- Assumption: Potential barrier through channel thickness is parabolic.

$$\Phi_{\min}(x) = \Phi_C - \frac{x^2}{R^2} (\Phi_C - \Phi_S)$$

- Modified current model:  $I_D \propto \frac{n_i^2}{N_A} \frac{\sqrt{\pi}}{2} R \cdot e^{\frac{\Phi_C}{V_t}} \cdot \frac{\operatorname{erf}\left(\sqrt{(\Phi_C - \Phi_S)/V_t}\right)}{\sqrt{(\Phi_C - \Phi_S)/V_t}}$

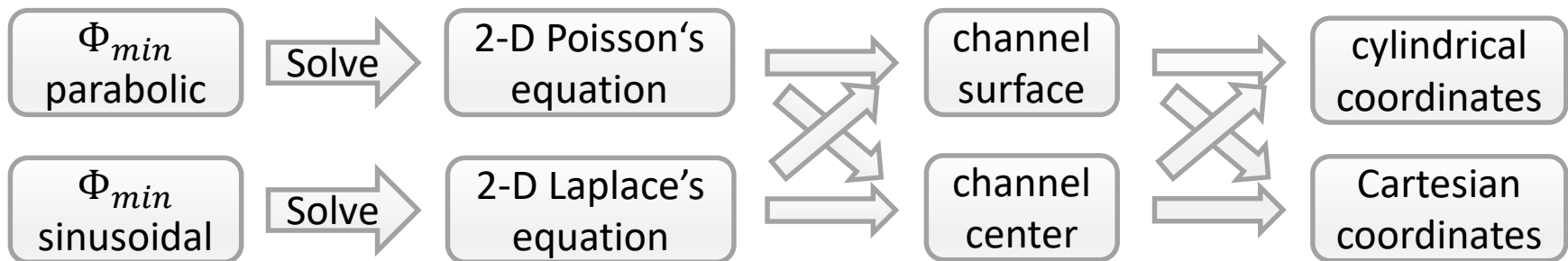


[3] Q. Chen et al., IEEE TED, Vol. 49, no. 6, pp. 1086-1090, June 2002.

## 2. Device dimensions dependent equivalent length

### Two independent derivation methods:

1. Method (=> slightly complicated):



Equate the potential drops  $\Phi_{min}(r) = \Phi_{min}(x)$  and compare the potential drops along the channel  $\Phi(r, z) \propto e^{\pm z/\lambda}$  with the so-called natural length  $\lambda$  [4,5,6].

Result for  $\Phi$  if  $\Phi_{min}$  is sinusoidal [7]:

$$\Phi_{DG} \approx \Phi_C \cdot \cos\left(\frac{x}{\lambda_{DG}}\right) \cdot \cosh\left(\frac{z_{DG}}{\lambda_{DG}}\right)$$

$$\Phi_{GAA} \approx \Phi_C \cdot J_0\left(\frac{r}{\lambda_{GAA}}\right) \cdot \cosh\left(\frac{z_{GAA}}{\lambda_{GAA}}\right)$$

$$z_{DG} \approx \frac{\lambda_{DG}}{\lambda_{GAA}} \cdot z_{GAA} \approx 1.53 \cdot z_{GAA}$$

[4] S.-H. Oh et al., IEEE EDL, Vol. 21, no. 9, pp. 445-447, September 2000.

[6] K. Suzuki et al., IEEE TED, Vol. 40, no. 12, pp. 2326-2329, Dec. 1993.

[5] R. H. Yan et al., IEEE TED, Vol. 39, no. 7, pp. 1704-1710, Jul. 1992.

[7] C. P. Auth et al., IEEE EDL, Vol. 18, no. 2 pp. 74-76, Feb. 1997.

## 2. Device dimensions dependent equivalent length

### Two independent derivation methods:

2. Method (=> simpler):

Device's electrostatics are represented by the subthreshold slope

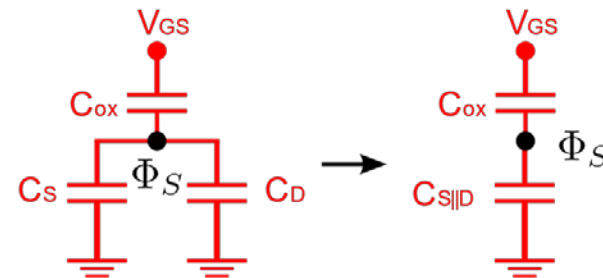
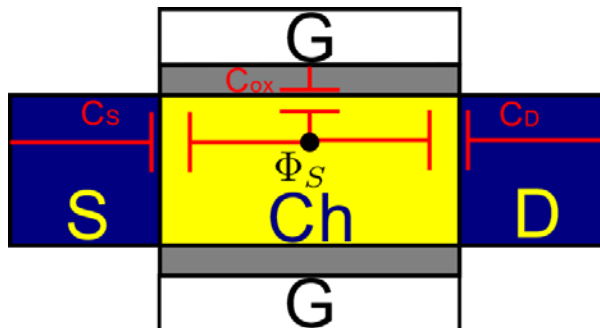
Equalize subthreshold slopes:

Lundstrom [8]:  $S_{sth} = \eta \log(10) V_T$

⇒ Ratio of capacitances must be equal!

$$S_{sth}^{DG} = S_{sth}^{GAA}$$

$$\eta^{-1} = \frac{\Phi_S}{V_{GS}} = \frac{\frac{1}{C_{S||D}}}{\frac{1}{C_{ox}} + \frac{1}{C_{S||D}}} = \frac{1}{1 + \frac{C_{S||D}}{C_{ox}}}$$



[8] Lecture: Lundstrom EE-612 F08

## 2. Device dimensions dependent equivalent length

### Two independent derivation methods:

Capacitance	DG	GAA
$C_{S,D}$	$\frac{\epsilon_{Si} W t_{ch}}{L_{DG}/2}$	$\frac{\epsilon_{Si} \pi R^2}{L_{GAA}/2}$
$C_{ox}$	$2 \frac{\epsilon_{ox} W}{t_{ox}} L_{DG}$	$2\pi \frac{\epsilon_{ox}}{\ln\left(1 + \frac{t_{ox}}{R}\right)} L_{GAA}$

Equivalent channel length:

$$L_{DG} = L_{GAA} * \sqrt{2} * \beta$$

with  $\beta = \sqrt{\frac{t_{ox}/R}{\ln(1+t_{ox}/R)}}$

In addition:

Equivalent channel width due to equivalent capacitances:  $W_{ch} = \frac{\pi R}{2} * \sqrt{2} * \beta$



## 2. Device dimensions dependent equivalent length

⇒ Simulation results match for the center potential:  $\Phi_{GAA}^C = \Phi_{DG}^C$

⇒ Simulation results don't match for the surface potential  $\Phi_S$ , subthreshold swing and DIBL.

⇒ Capacitance model of Lundstrom has its limitations.

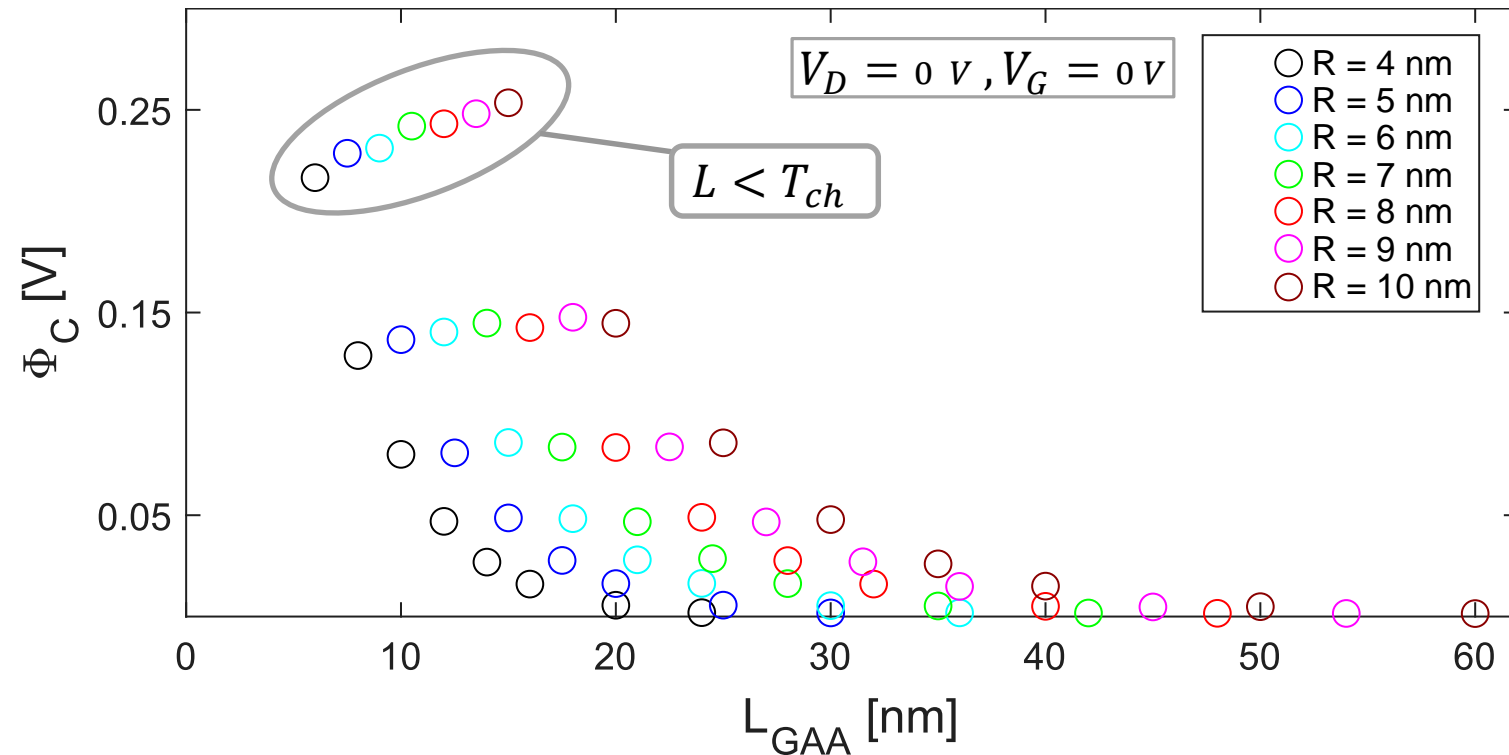
The first method helps out:

Solve the Laplace equation by assuming a sinusoidal shape through the channel thickness! Combining both methods lead to the best match for  $\Phi^S$ , swing and DIBL.

- Equivalent channel length:  $L_{DG} = L_{GAA} * 1.53 * \beta$  with  $\beta = \sqrt{\frac{t_{ox}/R}{\ln(1+t_{ox}/R)}}$
- Equivalent channel width:  $W_{ch} = \frac{\pi R}{2} * 1.53 * \beta$

### 3. Simulation & Compact Model Results

Center potential  $\Phi_C$  vs. channel length  $L_{GAA}$

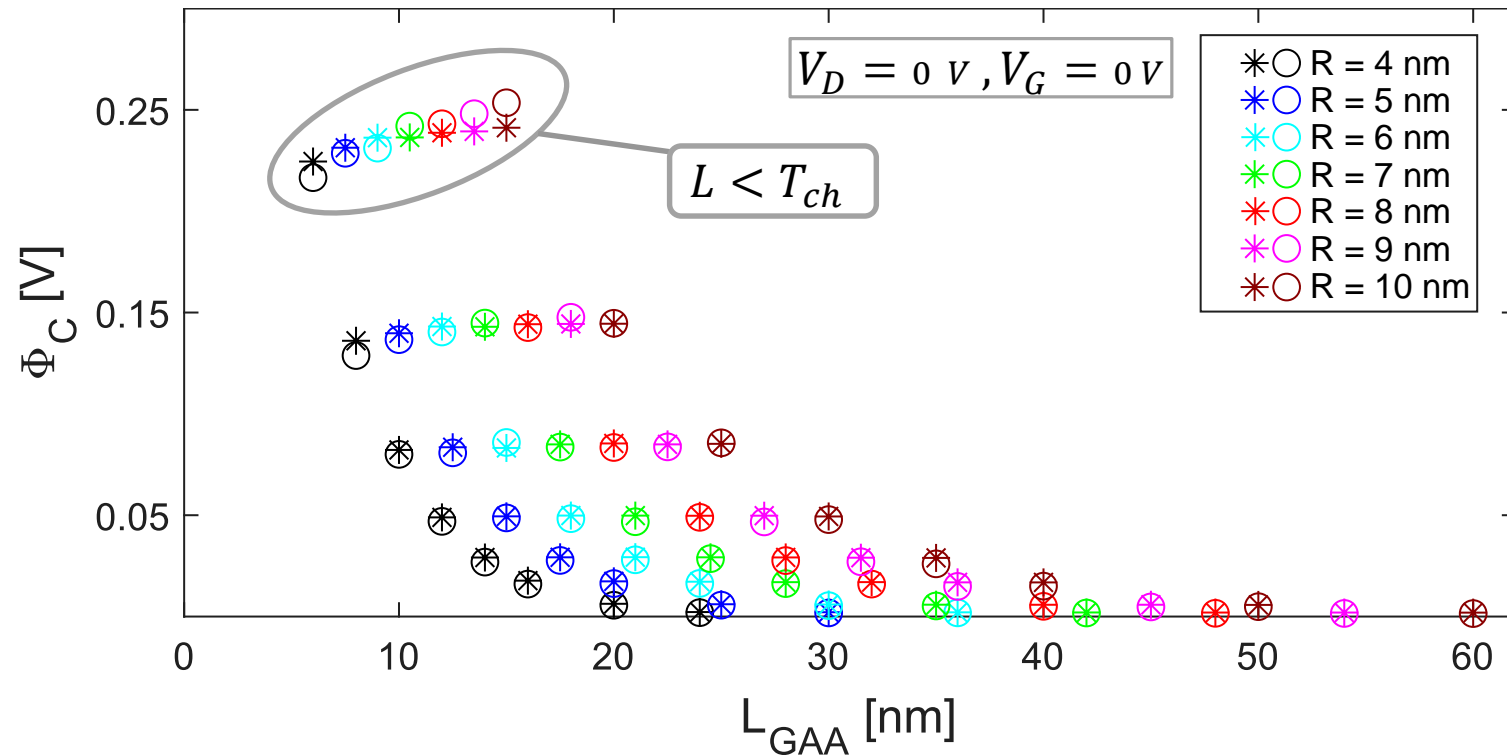


$L_{GAA} = 1.5R, 2R, 2.5R, 3R, 3.5R, 4R, 5R, 6R$

○ TCAD (GAA)   \* TCAD (DG)   + Model

# 3. Simulation & Compact Model Results

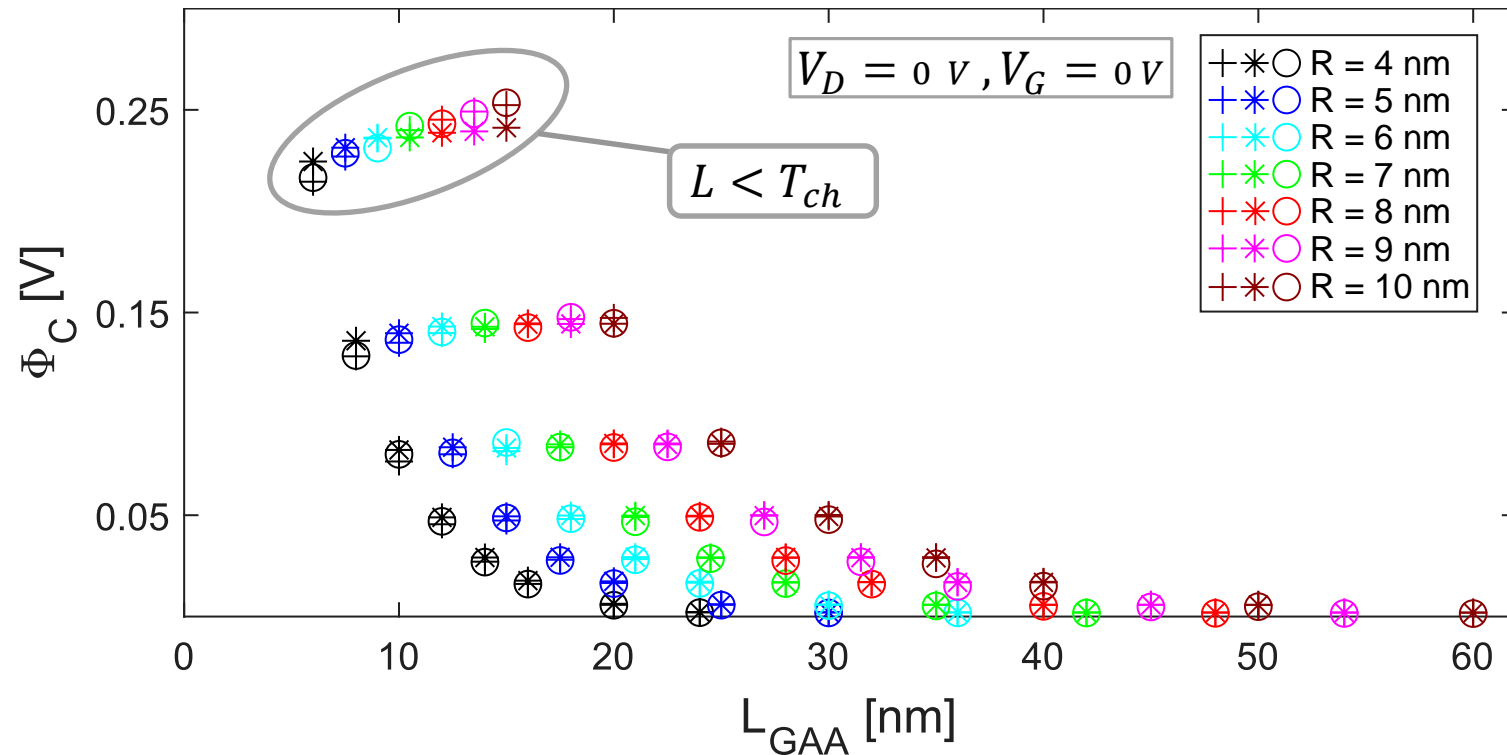
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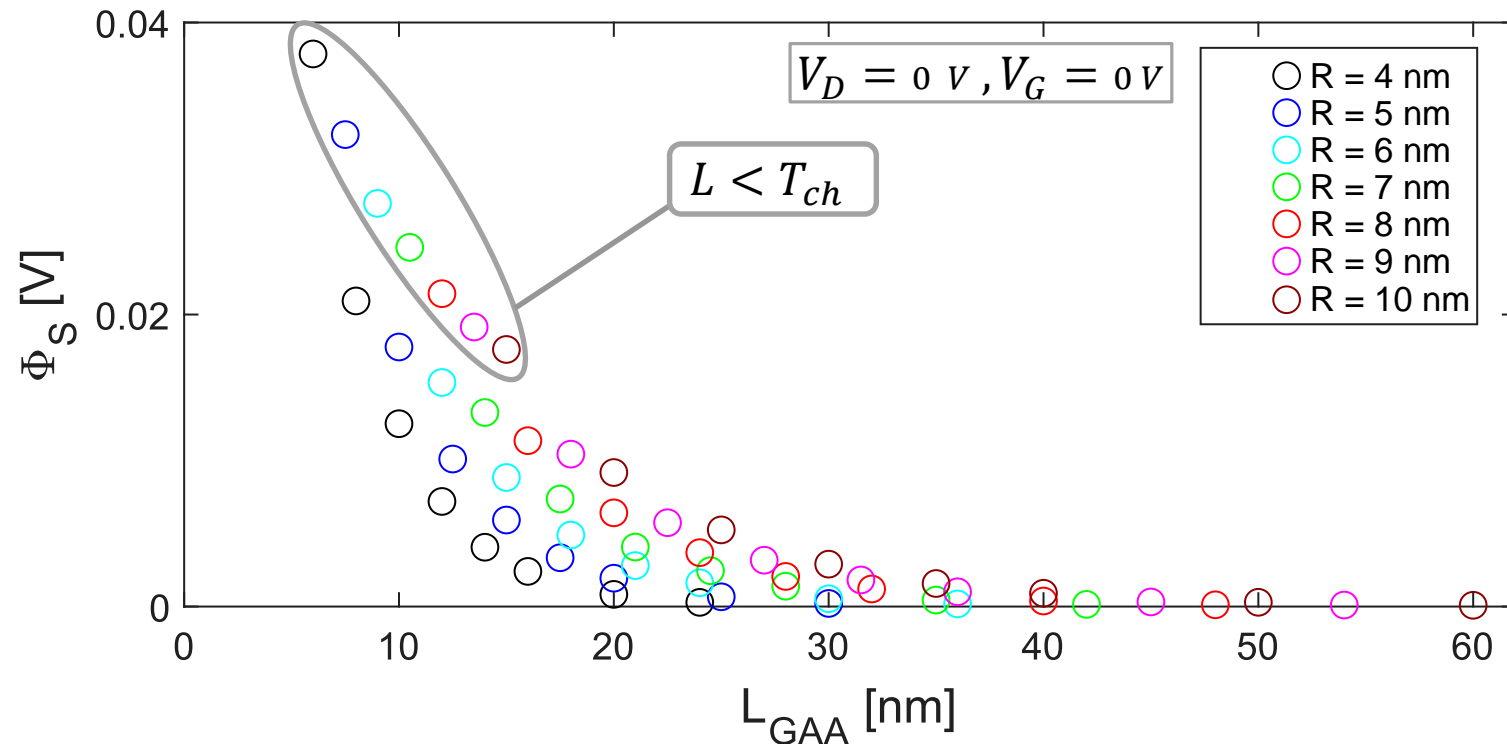
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Surface potential  $\Phi_S$  vs. channel length  $L_{GAA}$

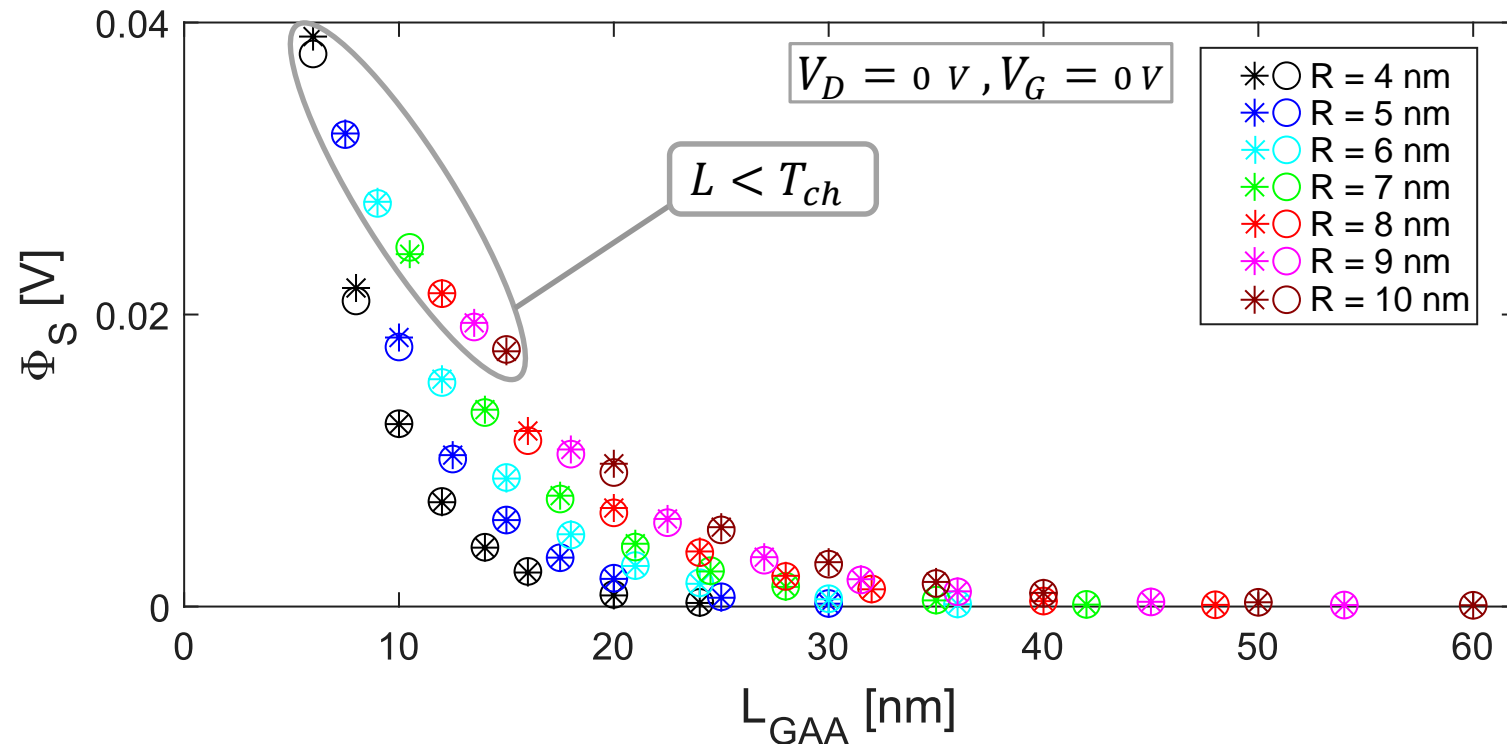


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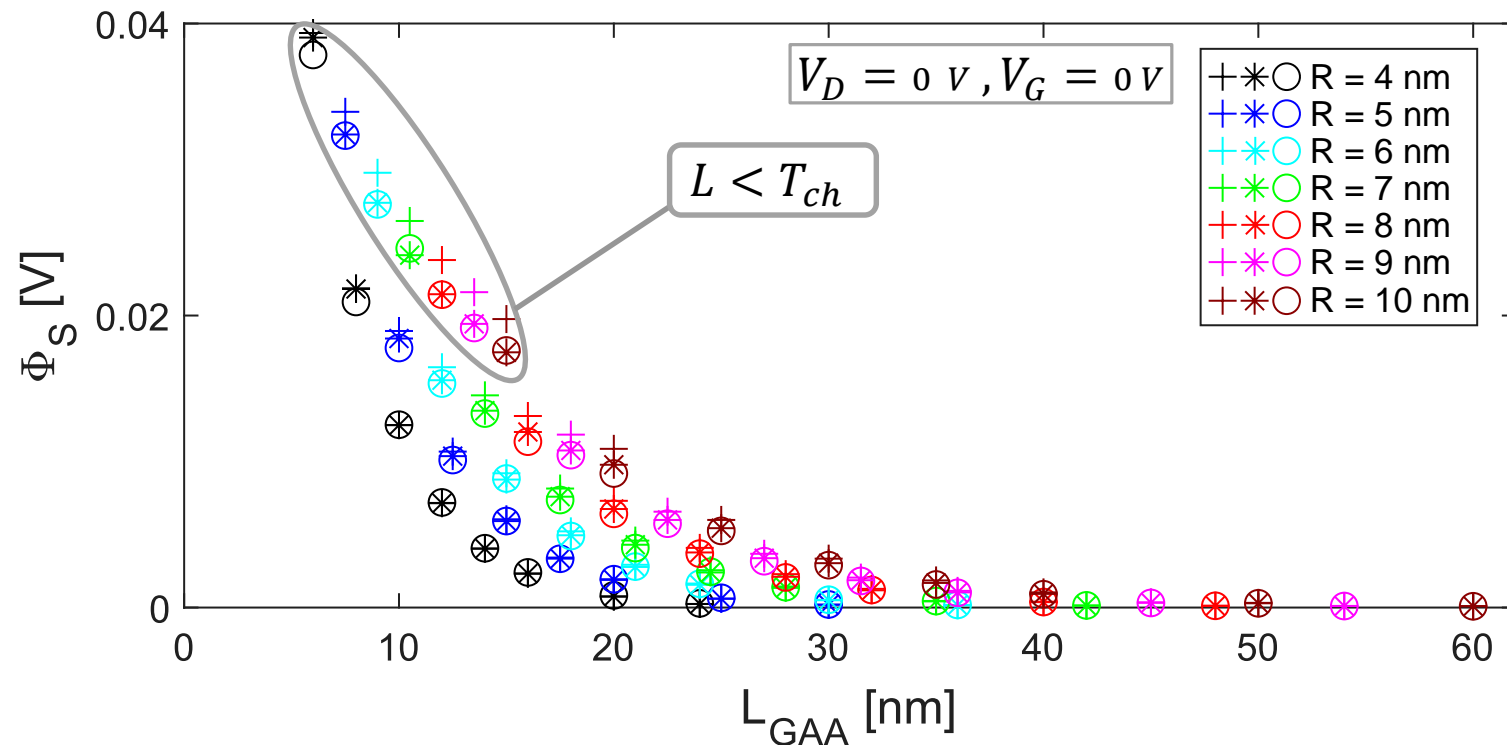


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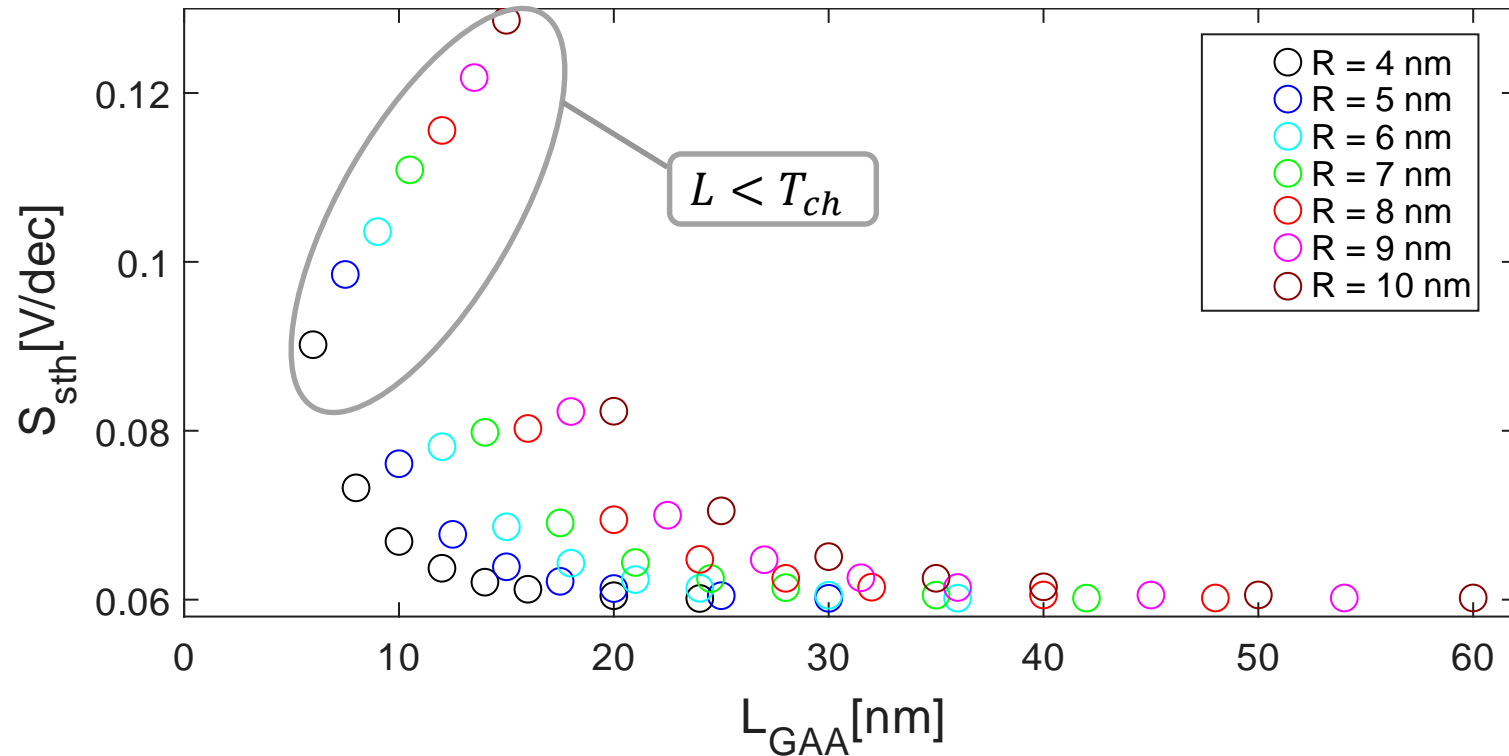


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Subthreshold Swing  $S_{sth}$  vs. channel length  $L_{GAA}$



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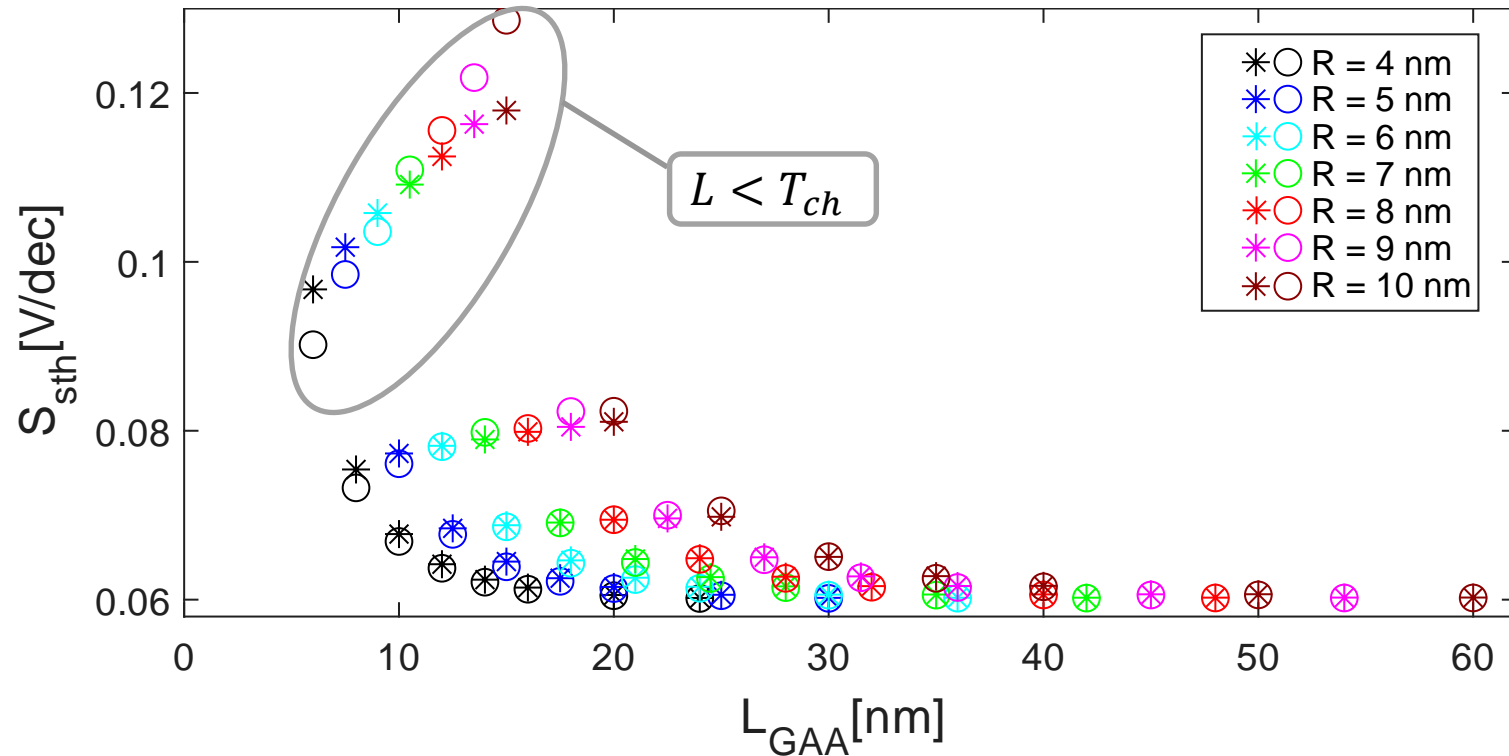
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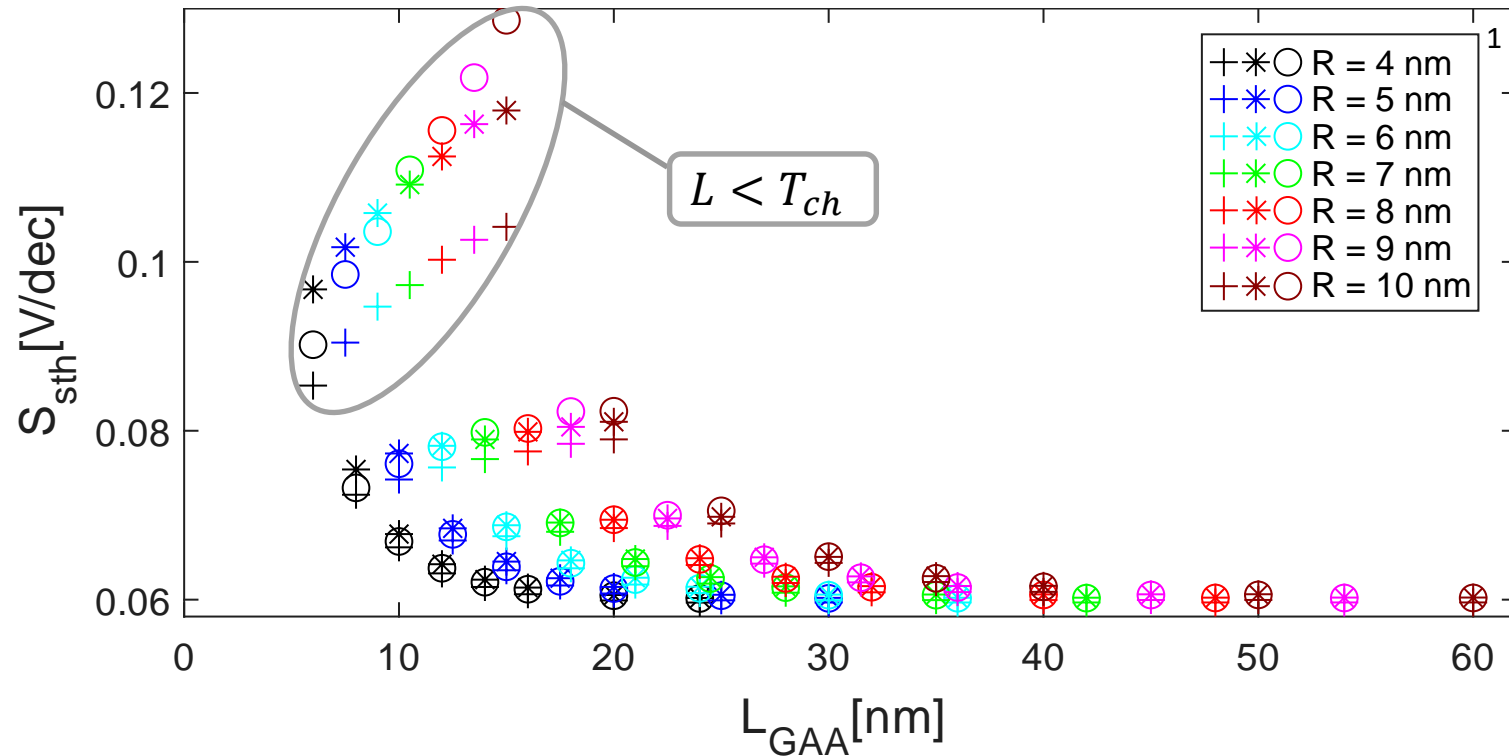
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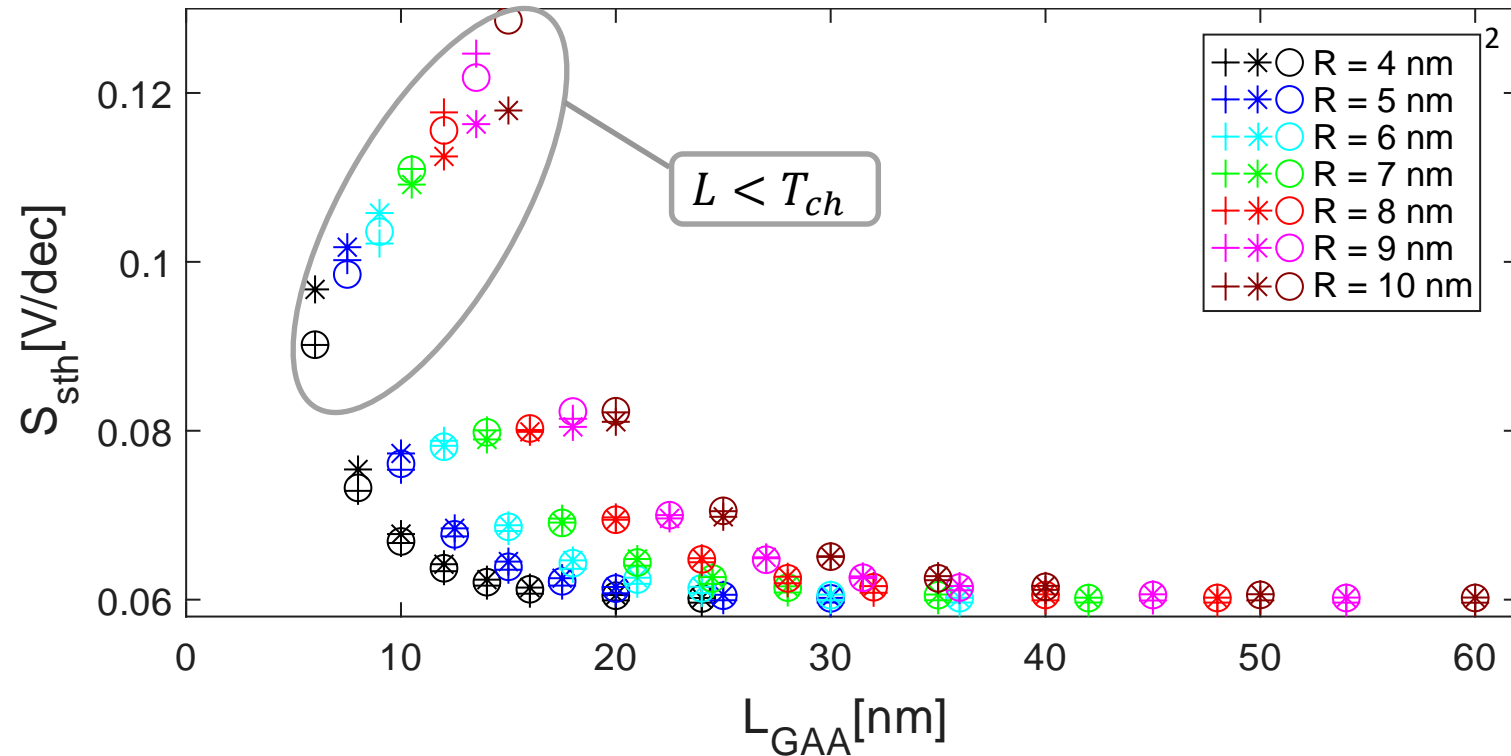
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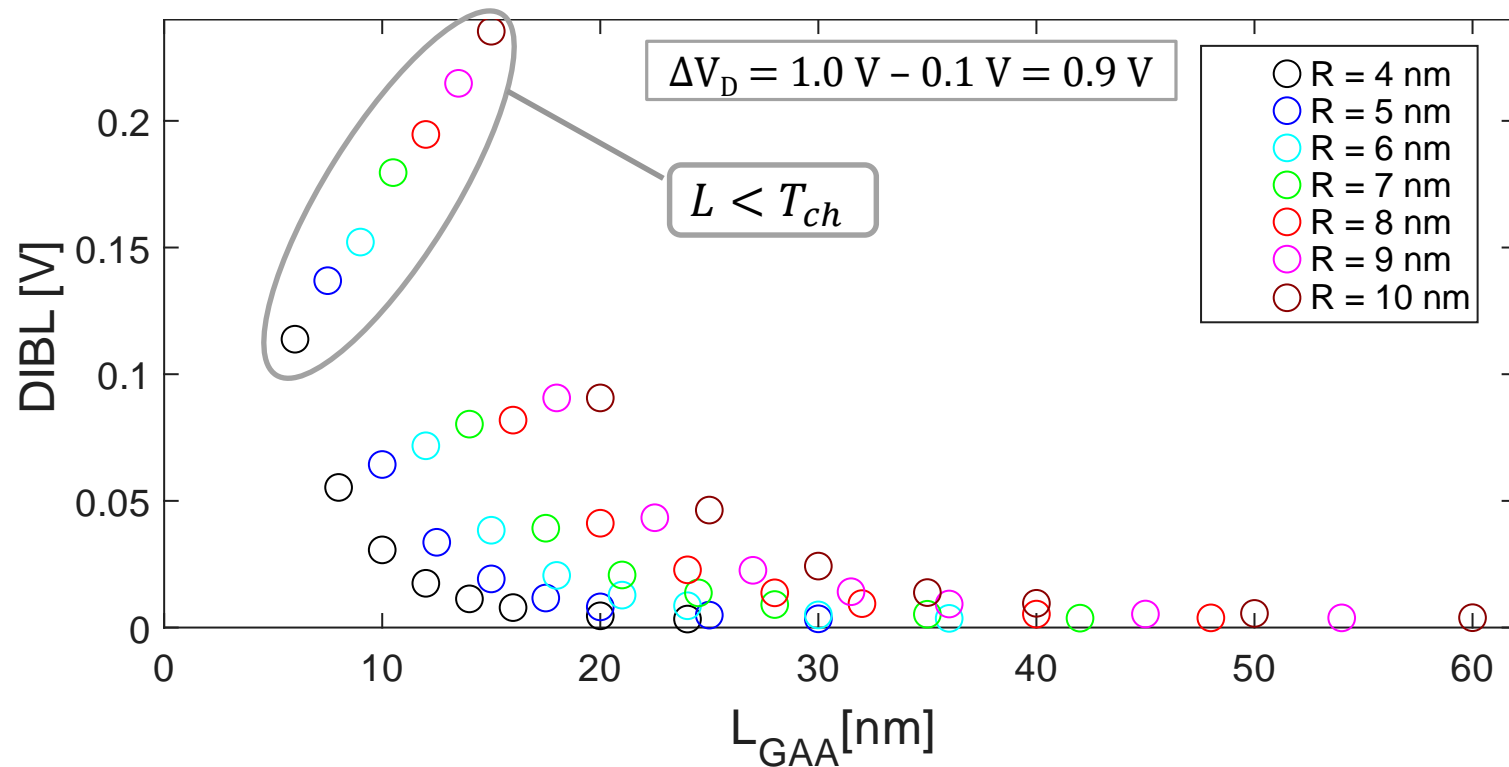
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Drain-induced barrier lowering (DIBL) vs. channel length  $L_{GAA}$



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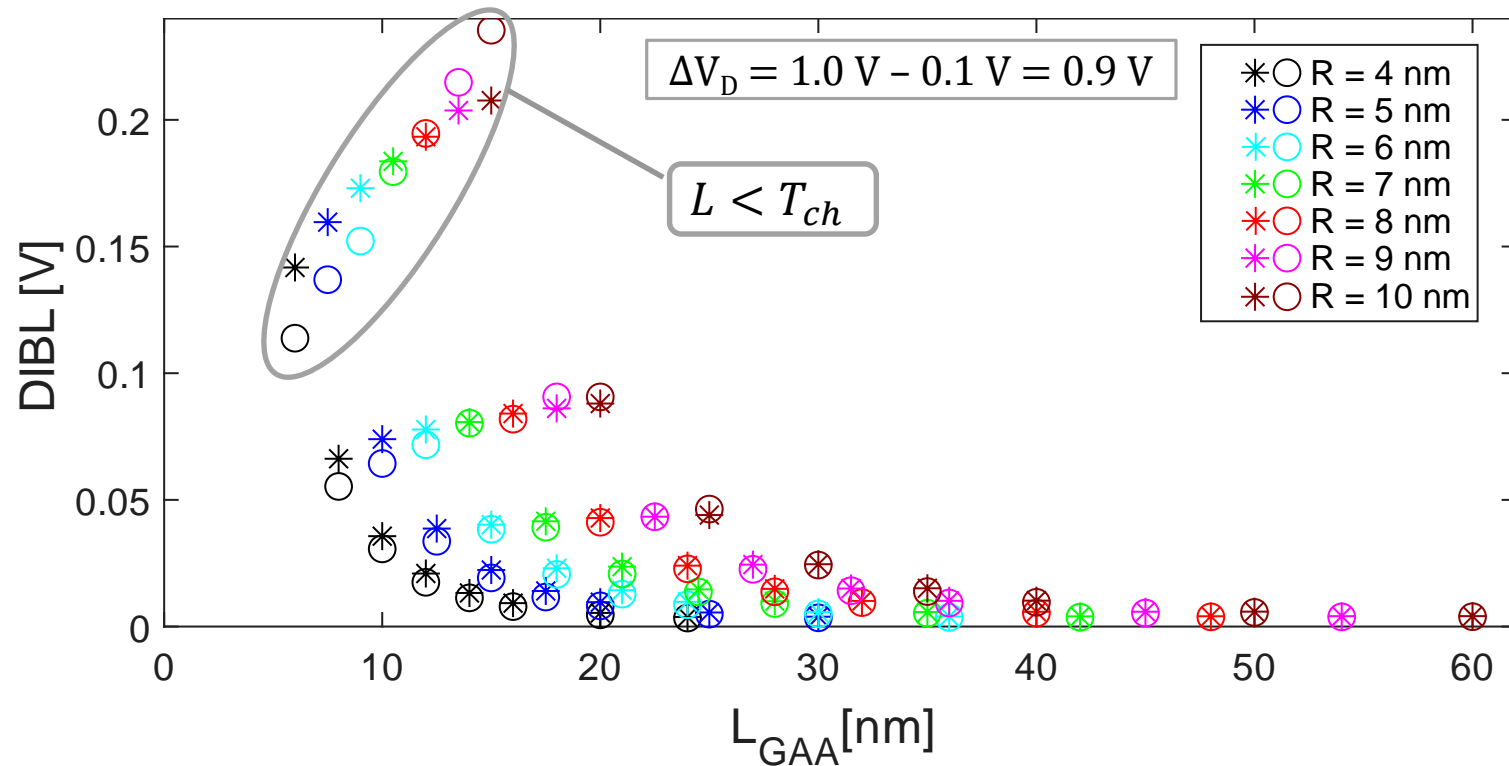
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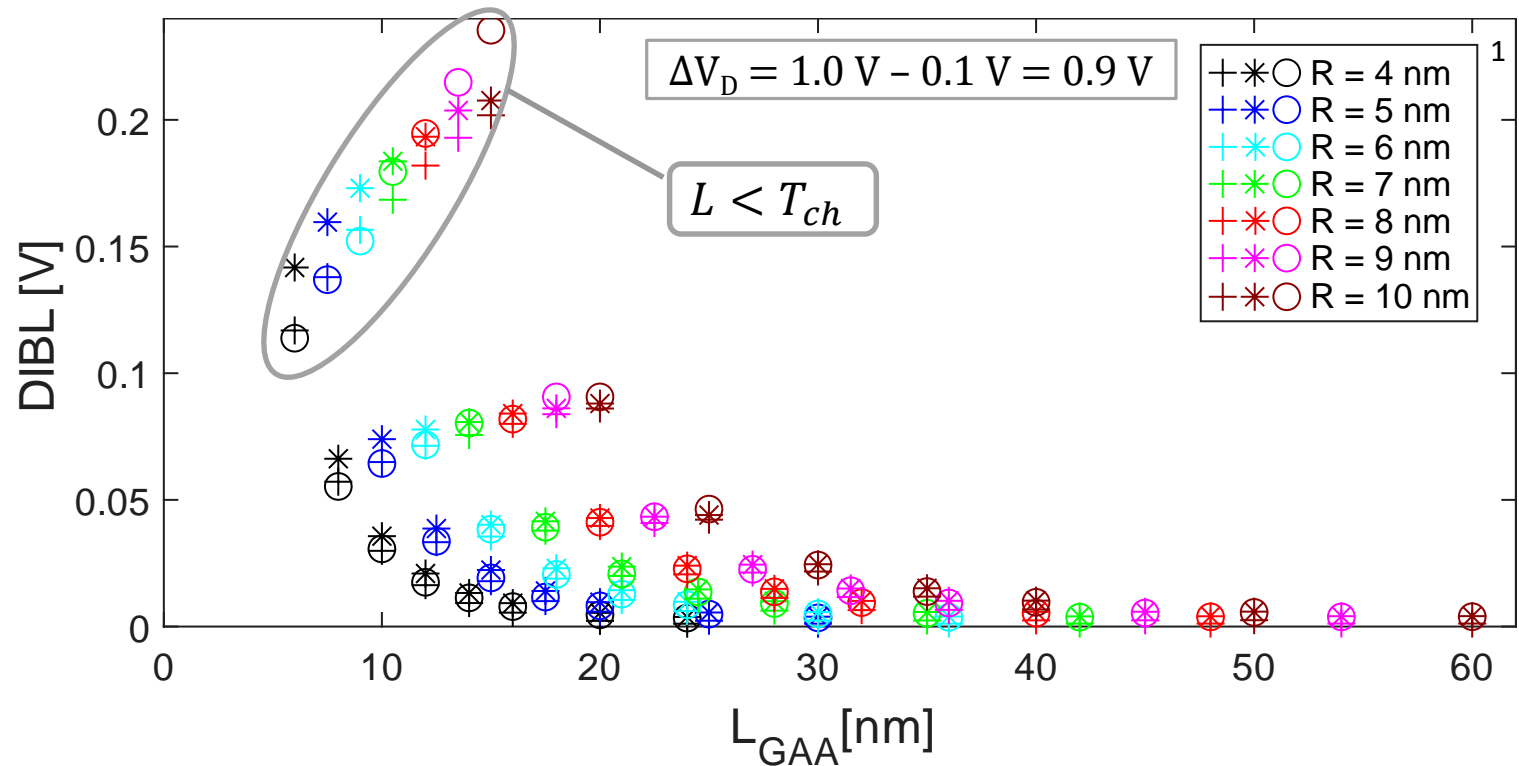
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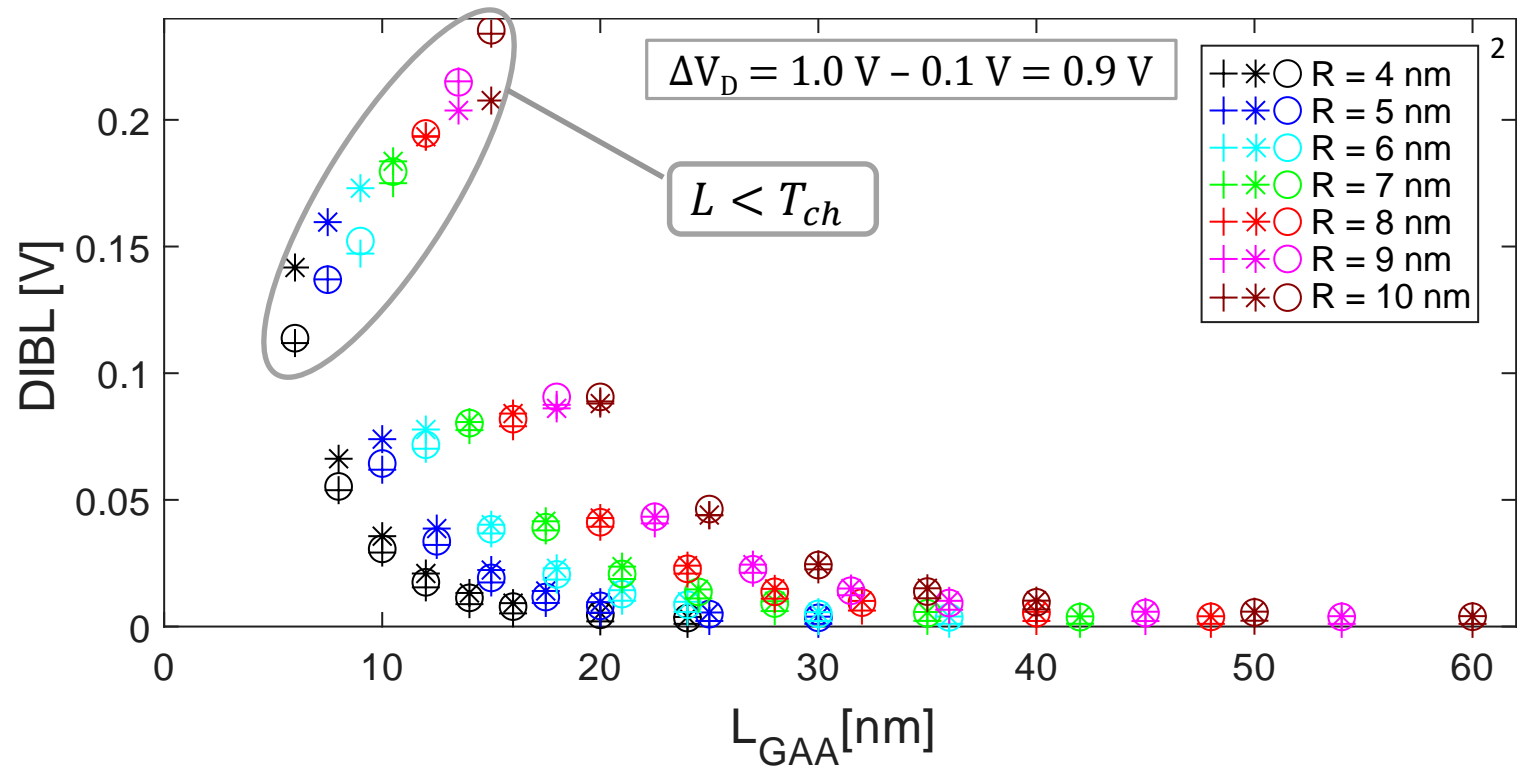
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## 4. Conclusion

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- The equivalent capacitance concept is presented to capture short channel GAA MOSFET electrostatic & behavior by DG MOSFET.
- It is shown that the method is working properly for subthreshold region in intrinsic and lightly doped channel.
- The center and surface potential ( $\phi_C$  &  $\phi_S$ ) need different equivalent values for the channel length.
- In subthreshold region where the leakage current mainly flows in the center, not only  $\phi_C$  but also  $\phi_S$  has significant influence on the electrostatic and characteristics.
- Outlook: The method is under development for above threshold short channel devices.