

# Global Geometrical Scaling in BSIM6

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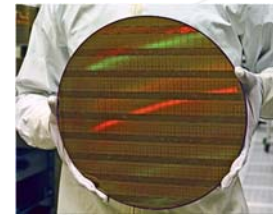
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Dec. 12<sup>th</sup>, 2012

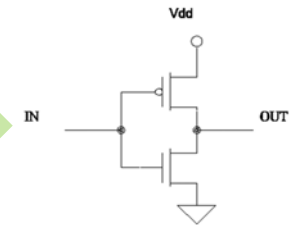
MOS-AK San Francisco



# SPICE Transistor Modeling

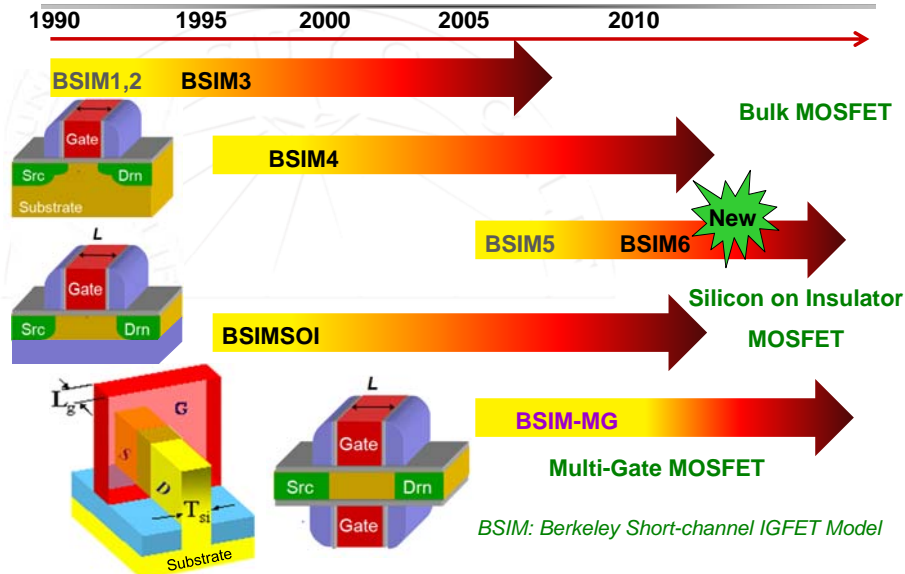


Medium of information exchange



- **Simulation Time**
  - ~ 10 $\mu$ s per DC data point
  - No complex numerical method allowed
- **Accuracy requirements**
  - ~ 1% RMS Error after fitting
- **Excellent Convergence**
- **Example: BSIM-CMG**
  - 5,000 lines of VA code
  - 50+ parameters
  - Open-source software implemented in major EDA tools

# BSIM Family of Compact Device Models



# BSIM6: Charge based MOSFET model

- **BSIM6 – Next BSIM Bulk MOSFET model**
  - Charge based core derived from Poisson’s solution
  - Real device effects (SCE, CLM etc.) from BSIM4
  - Parameter names matched to BSIM4
- **Physical Capacitance model**
  - Short channel CV–Velocity saturation & CLM
- **Symmetry**
  - Currents & derivatives are symmetric @ VDS=0
  - Capacitances & derivatives are symmetric @VDS=0
  - Provide accurate results in Harmonic Distortion simulation
- **Continuous** in all regions of operations
- **Better Statistical Modeling** using physical parameters

## Physics of BSIM6 Model

- Gauss' Law

$$V_G - V_{FB} - \Psi_S = -\frac{Q_{si}}{C_{ox}} = -\frac{Q_i + Q_b}{C_{ox}}$$

- Poisson's solution for long channel MOSFET

$$\frac{Q_{si}}{\Gamma C_{ox} \sqrt{V_t}} = \mp \sqrt{e^{-\frac{\Psi_S}{V_t}} + \frac{\Psi_S}{V_t} - 1 + e^{-\frac{2\Phi_F + V_{ch}}{V_t}} \left( e^{\frac{\Psi_S}{V_t}} - \frac{\Psi_S}{V_t} - 1 \right)}$$

- Bulk charge density is given by

$$\frac{Q_b}{\Gamma C_{ox} \sqrt{V_t}} = \mp \sqrt{e^{-\frac{\Psi_S}{V_t}} + \frac{\Psi_S}{V_t} - 1}$$

- Combining these, we have

$$V_G - V_{FB} - \Psi_S = -\frac{Q_i}{C_{ox}} \pm \Gamma \sqrt{V_t \left( e^{-\frac{\Psi_S}{V_t}} + \frac{\Psi_S}{V_t} - 1 \right)}$$

5

## Physics of BSIM6 Model

- Defining Pinch-off potential  $\Psi_p = \Psi_S$ , when  $Q_i = 0$

$$V_G - V_{FB} - \Psi_p = \text{sign}(\Psi_p) \Gamma \sqrt{V_t \left( e^{-\frac{\Psi_p}{V_t}} + \Psi_p - 1 \right)}$$

$\Psi_p$  is evaluated from implicit equation

$$-\frac{Q_i}{\Gamma C_{ox} \sqrt{V_t}} = \sqrt{\frac{\Psi_S}{V_t} + e^{-\frac{\Psi_S - 2\Phi_F - V_{ch}}{V_t}} - 1} - \sqrt{\frac{\Psi_S}{V_t}}$$

- For  $\Psi_S > \text{few } V_t$ , we have

$$-\frac{Q_i}{C_{ox}} = n_q (\Psi_p - \Psi_S)$$

$n_q$  is the slope factor

- Inversion Charge linearization

\*Ref.: Tsividis book & J.M. Sallese et al., Solid State Electronics

6

## Physics of BSIM6 Model

- Using linearization approach and normalization

ACM/EKV/BSIM5 ignored the circled term

$$\ln(q_i) + \ln \left[ \frac{2n_q}{\gamma} \left( \frac{2n_q}{\gamma} q_i + 2\sqrt{-2q_i + \psi_p} \right) \right] + 2q_i = \psi_p - 2\phi_f - V_{ch}$$

- No approximation to solve the charge equation compared to other models.

- Solved the charge equation analytically

7

## Drain current with velocity saturation

- Drain current

$$I_D = I_{drift} + I_{diff} = \mu W \left( -Q_i \frac{d\Psi_S}{dx} + V_t \frac{dQ_i}{dx} \right)$$

- Mobility model (ensures symmetry)

$$I_D = \frac{\mu_v}{\sqrt{1 + \left( \frac{\mu_v}{v_{sat}} \frac{d\Psi_S}{dx} \right)^2}} W \left( -Q_i \frac{d\Psi_S}{dx} + V_t \frac{dQ_i}{dx} \right)$$

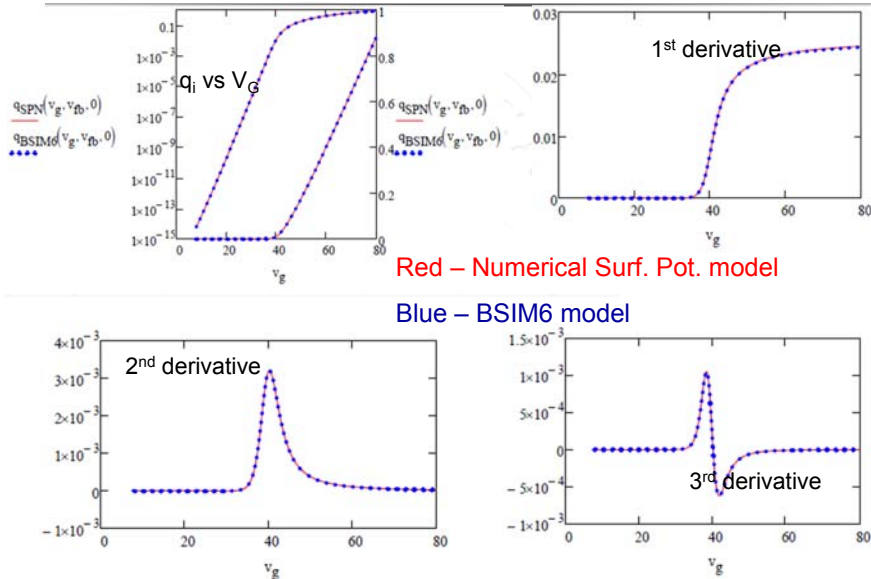
$$-\frac{Q_i}{C_{ox}} = n_q (\Psi_p - \Psi_S), q = \frac{-Q_i}{2n_q C_{ox} V_t}, i_d = \frac{I_D}{2n_q \frac{W}{L} \mu_v C_{ox} V_t^2}, \lambda_c = \frac{2\mu_v V_t}{v_{sat} L}$$

- Using charge linearization & normalization

$$i_d = \frac{(q_s^2 + q_d) - (q_d^2 + q_s)}{\frac{1}{2} \left( 1 + \sqrt{1 + [\lambda_c (q_s - q_d)]^2} \right)}$$

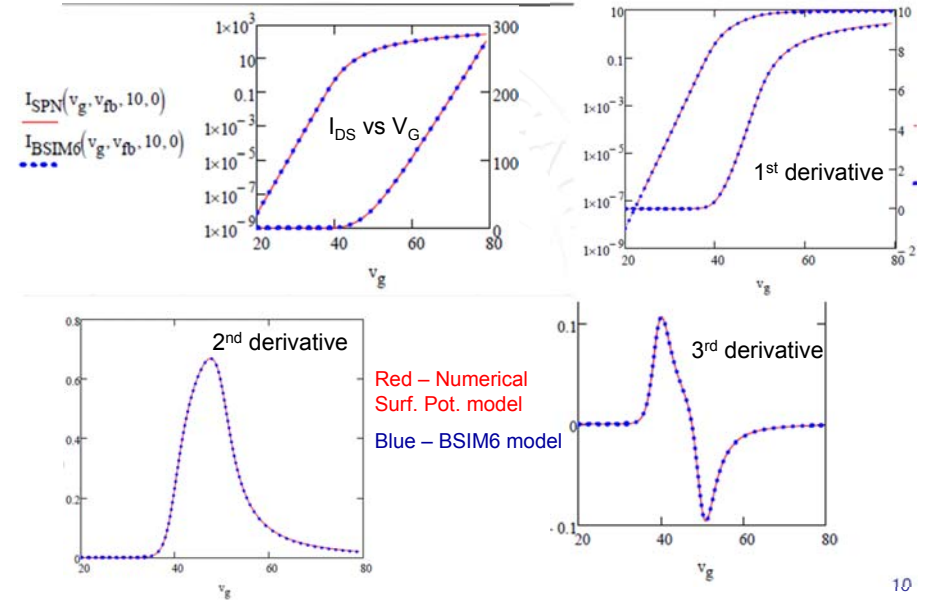
8

## Normalized $Q_i$ - $V_G$ & derivatives



9

## Normalized $I_{DS}$ - $V_{GS}$ & derivatives



10

## Mobility Model

- Mobility model has been adopted from BSIM4

$$\mu_{eff} = \frac{U0 \cdot f(L_{eff})}{1 + (UA + UC \cdot V_{bsx}) \cdot E_{eff}^{EU} + \left[ \frac{1}{2} \left( 1 + \frac{q_{is}}{q_{bs}} \right) \right]^{UCS}}$$

BSIM4

$$\mu_{eff} = \frac{U0 \cdot f(L_{eff})}{1 + (UA + UC \cdot V_{bsx}) \cdot E_{eff}^{EU} + \left[ \frac{1}{2} \left( 1 + \frac{q_{is}}{q_{bs}} \right) \right]^{UCS}}$$

BSIM6

where

$$\eta = \begin{cases} \frac{1}{2} \cdot ETAMOB & \text{for NMOS} \\ \frac{1}{3} \cdot ETAMOB & \text{for PMOS} \end{cases}$$

$$E_{effs} = 10^{-8} \cdot \left( \frac{q_{bs} + \eta \cdot q_{is}}{\epsilon_{ratio} \cdot TOX} \right)$$

MV/cm

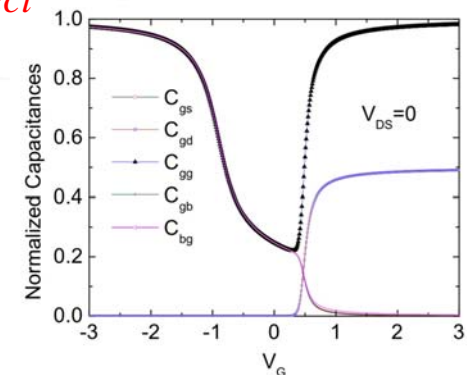
$$V_{dsx} = \sqrt{V_{ds}^2 + 0.01} - 0.1$$

$$V_{bsx} = - \left[ V_s + \frac{1}{2} (V_{ds} - V_{dsx}) \right]$$

11

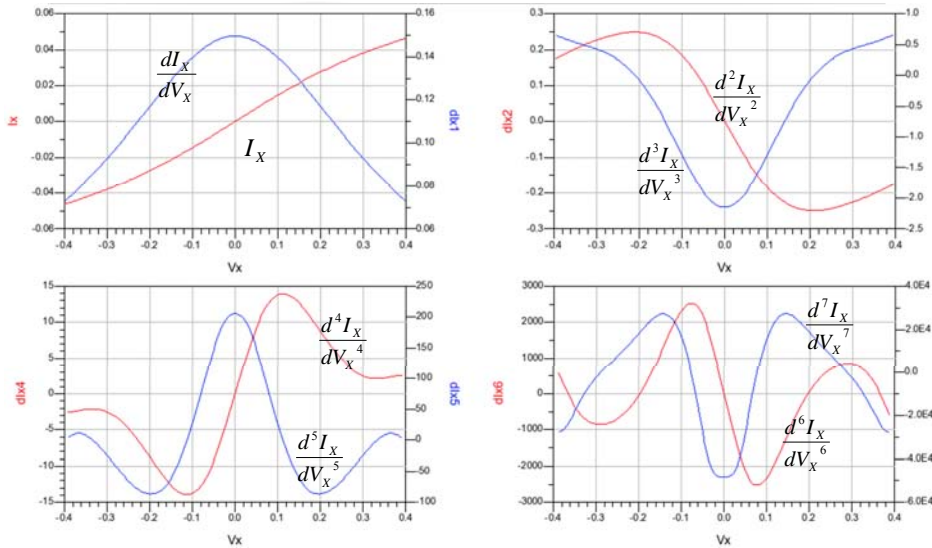
## CV Model

- Physical Capacitance Model
- Poly-depletion & *Quantum Mechanical Effect*
- Channel Length Modulation
- *Velocity Saturation Effect*
- Charge conservation



# $I_{DS}-V_X$ Gummel Symmetry

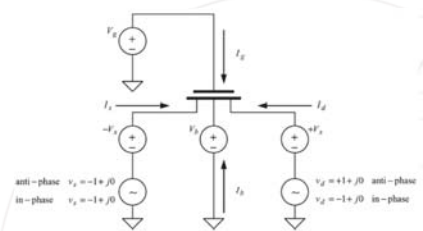
$I_X$  vs  $V_X$  ( $V_D=V_X$  &  $V_S=-V_X$ )



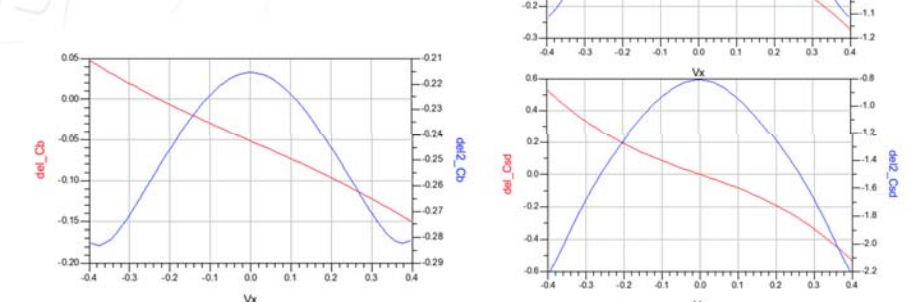
All derivatives are continuous at  $V_{DS}=0$

# AC Symmetry test

(C. McAndrew, IEEE TED, 2006)



Capacitance & derivatives are symmetric



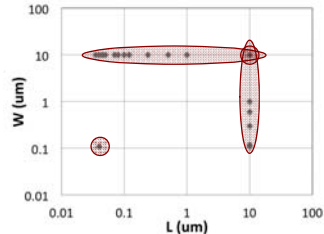
Capacitances and derivatives are continuous at  $V_{DS}=0$

Evaluation of the BSIM6 Model

## General Information

- BSIM6 is validated against ST 40nm Bulk CMOS Technology Measurements
- Almost the same Parameter Extraction Procedure with BSIM4 is followed

### Minor Adjustments



- The results are in form of Normalized Quantities

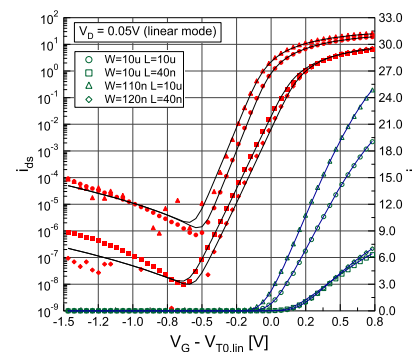
$$i_{ds} = \frac{I_{DS}}{I_{spec}}, \quad g_m = \frac{G_m}{G_{spec}}, \quad g_{ds} = \frac{G_{ds}}{G_{spec}}$$

$$G_{spec} = \frac{I_{spec}}{U_T}$$

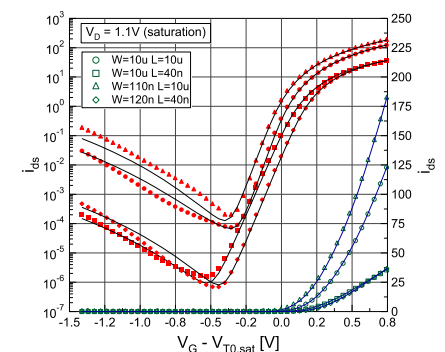
Evaluation of the BSIM6 Model

## Evaluation of the Model for the Corner DUTs – 1/3

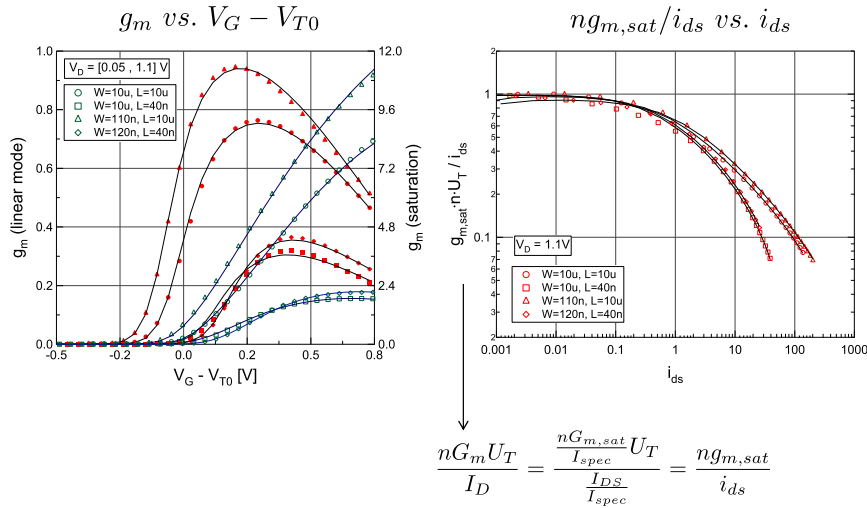
$i_{ds,lin}$  vs.  $V_G - V_{T0,lin}$



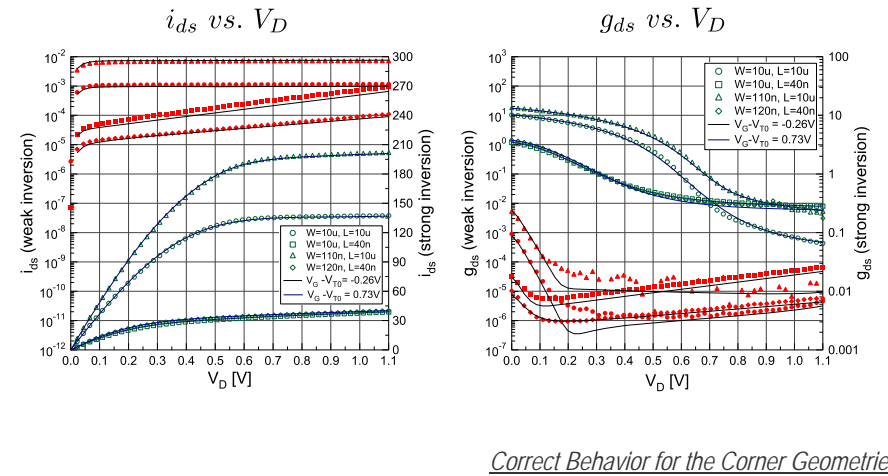
$i_{ds,sat}$  vs.  $V_G - V_{T0,sat}$



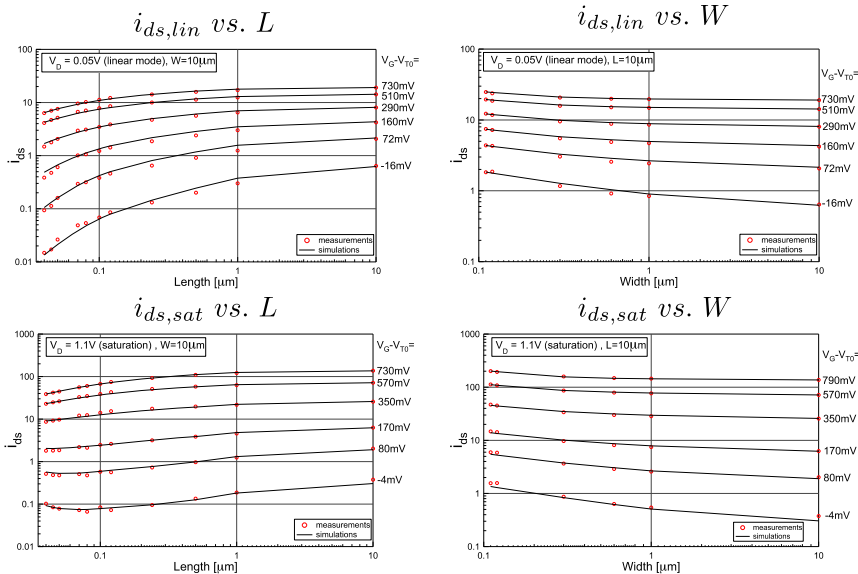
## Evaluation of the Model for the Corner DUTs – 2/3



## Evaluation of the Model for the Corner DUTs – 3/3



## Evaluation of the Model's Scalability – 1/2

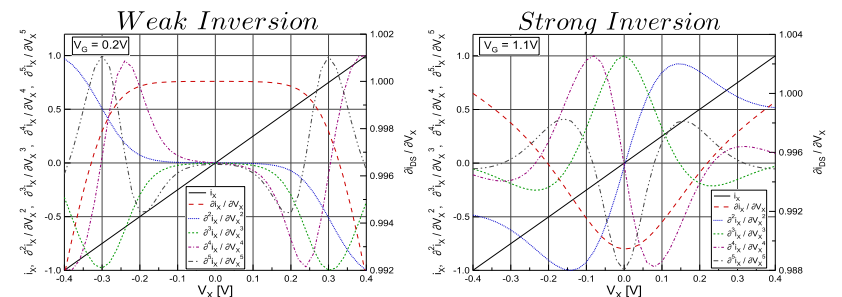


## Study of the Model's Symmetry

- Gummel Symmetry Test (GST) in Weak & Strong Inversion
- Test BSIM6 for  $I_X$  Current and its Derivatives up to 5<sup>th</sup> Degree
- Quantities are Normalized to their Maximum Values

$I_X = I_D - I_S$  vs.  $V_X = V_D - V_S$ , when  $V_D = -V_S$

$$i_X = \frac{I_X}{\max(I_X)} \quad \text{and} \quad \frac{\partial^n i_X}{\partial V_X^n} = \frac{(\partial^n I_X) / \partial V_X^n}{\max(\partial^n I_X / \partial V_X^n)}$$



*Smooth behavior around  $V_{DS}=0V$*

## BSIM6 model summary

- Rapid development: Released **BSIM6.0.0-beta8B** in **Sept. 2012**
- Charge based physical compact model
  - Physical effects & Parameter names matched to BSIM4
  - Smooth charge/current/capacitance & derivatives
- **Symmetric and continuous around  $V_{DS}=0$** 
  - Fulfills Gummel symmetry and AC symmetry
  - Shows accurate slope for harmonic balance simulation
- BSIM4's **extraction methodology** can be easily used for BSIM6 – **fast deployment & lower cost**
- Under standardization review in CMC

21

## Acknowledgement

- Models users
  - SOITEC
- EDA Vendors
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  - Pragma Kushwaha
  - Chadan Yadav
  - Shantanu Agnihotri
- LETI
- ST Microelectronics
- Analog Devices
- Texas Instruments
- TSMC
- Global Foundries
- All other CMC Members

22

## BSIM6 References

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23