

# Low-Frequency Noise Modeling at Low Temperature with the EKV3 Compact Model

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# Outline

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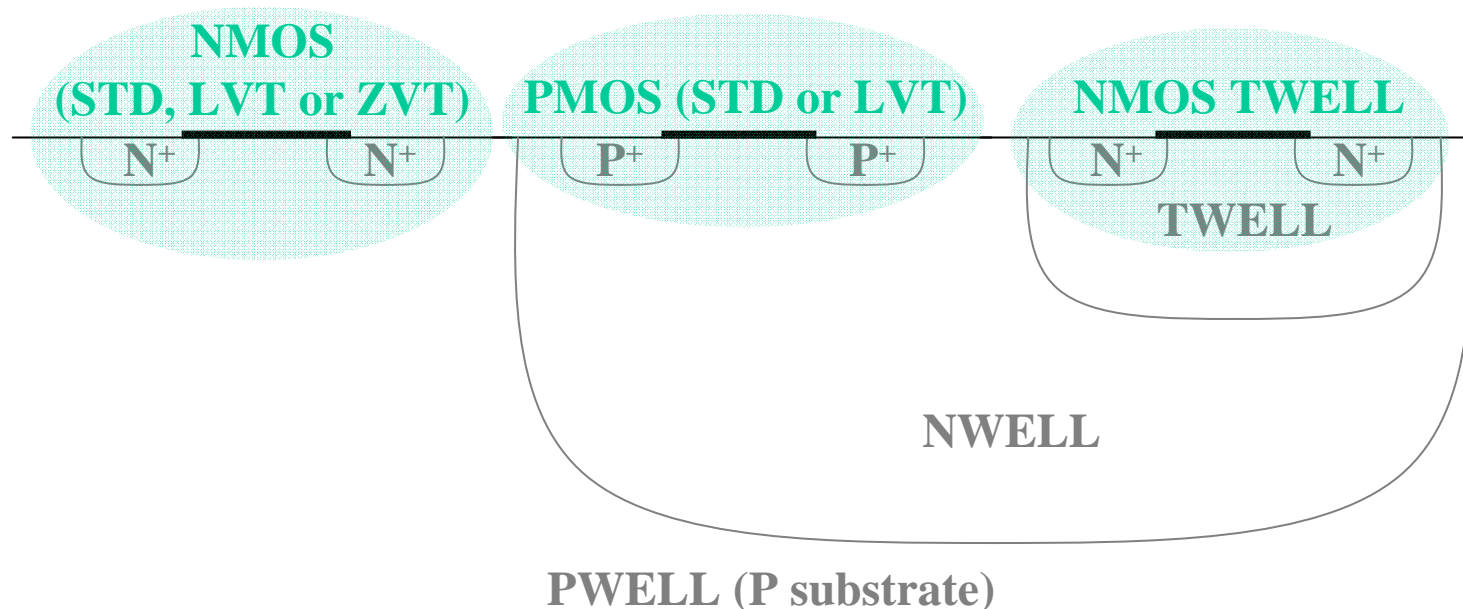
- **Introduction**
- **CMOS process and characterization**
- **Low frequency (LF) noise measurements at room & low temperature and physical models**
- **Compact modeling of LF noise with EKV3**
- **Conclusion**

# Introduction: aim of this work

- **Design of hybrid CMOS read-out circuits for night vision using high performance infrared (IR) detectors**
- **IR detectors and CMOS circuits cooled down to 77 K**
- **Difficulties: low temperature (LT) & analog circuits (weak/moderate inversion)**
- **IC design with 0.8, 0.5 and 0.35  $\mu\text{m}$  CMOS and circuit simulation with the EKV2.6 compact model**
- **More and more transistors in the pixel, need for more and more advanced CMOS processes**
- **0.18  $\mu\text{m}$  process: new effects, e.g. INWE (STI), DITS (pockets)**
- **EKV3 is an accurate compact model for LT analog circuits design, Cryogenics, in press, 2009**
- **This work: evaluation of the EKV3 LF noise model**

# CMOS process

- Commercial process for Analog / Digital / RF applications
- Not optimized for LT operation
- Dual gate:
  - ✓ 0.18  $\mu\text{m}$  - 1.8 V -  $T_{\text{ox}}=3.3$  nm
  - ✓ 0.35  $\mu\text{m}$  - 3.3 V -  $T_{\text{ox}}=6.5$  nm
- Multi-Vt: standard (STD), low Vth (LVT), zero Vth (ZVT)
- Triple well
- Twelve MOSFET



# DC characterization and LFN measurements

## DC characterization

- 1<sup>st</sup> step before LF noise measurements
- Standard and specific effects
- Id, Gm, Gmb, Gds
- Temperature range: 77 K - 300 K

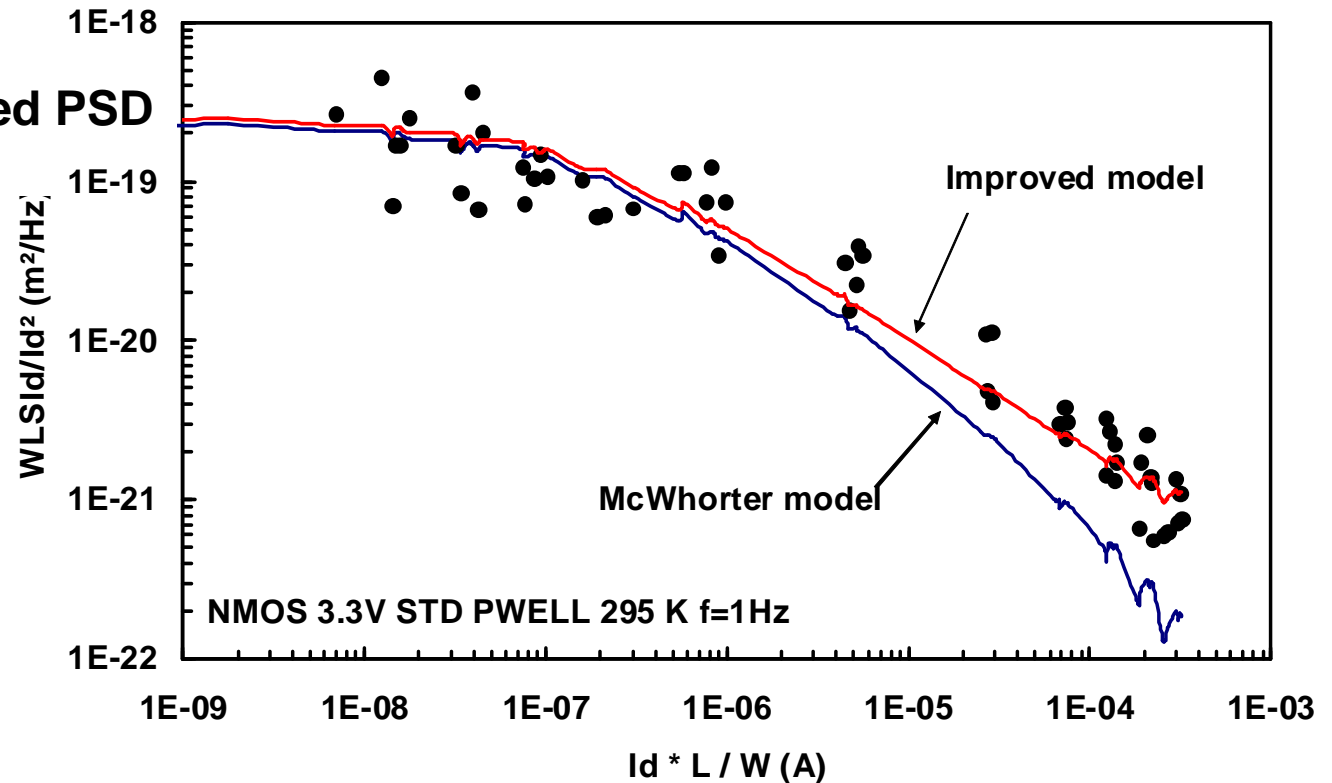
## LF noise measurements

- Automatic current fluctuations meas. on up to 6 devices inside a cryostat
- Specific computer-controlled system with programmable biasing amplifiers
- Transistors biased in saturation:  $V_{ds}=V_{DD}$  as in analog circuits
- $L=L_{min} - 20 \mu\text{m}$  ;  $W=W_{min} - 20 \mu\text{m}$
- $1/f^\gamma$  noise with  $\gamma = 1.0 \pm 0.1$

# Noise measurements at room temperature: Hooge, standard or improved McWhorter's model?

NMOSFET 3.3 V  
295 K

Normalized PSD



- Plateau in weak inversion: Hooge mobility fluctuation model not applicable
- McWhorter's carrier number model applicable, but has to be improved in strong inversion
- Same model applies experimentally for PMOSFET

# The improved McWhorter's LF noise model

## 1 - Standard McWhorter carrier number fluctuations ( $\Delta N$ )

$$SI_d = \left[1 + \alpha \mu C_{ox} \frac{I_d}{G_m}\right]^2 G_m^2 S_{Vfb}(f) \quad [A^2/Hz]$$

## 2 - Correlated mobility fluctuations ( $\Delta\mu$ ) at high current

$$S_{Vfb}(f) = \frac{kT q^2 \lambda N_t(E_F)}{WL C_{ox}^2} \frac{1}{f^\gamma} \quad [V^2/Hz]$$

$S_{Vfb}$ : flat-band voltage fluctuations

$N_t$ : oxide trap volume density per unit energy at  $E_F$  ( $eV^{-1} cm^{-3}$ )

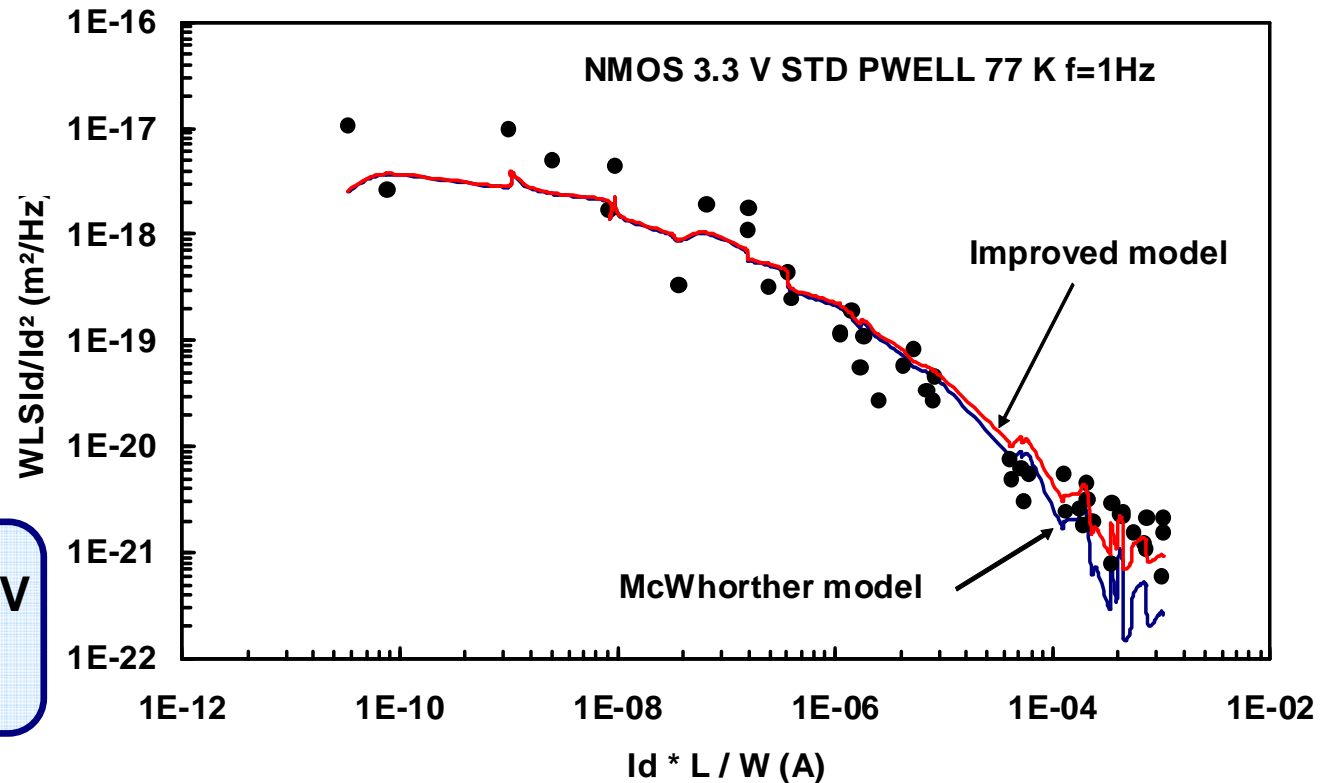
$\lambda$ : tunnel attenuation distance (0.1 nm)

$\alpha$ : Coulomb scattering coefficient at RT (V s/C)  $\sim 10^4$  for electrons,  $10^5$  for holes

(3.3 V STD n-MOSFETs:  $\alpha=7 \times 10^3$  at 295 K)

# Noise measurements at 77 K

NMOSFET 3.3 V  
77 K



- Improved McWhorter's model still applicable at low temperature
- Lower  $\alpha$  Coulomb scattering coefficient at LT ( $9 \times 10^2$  at 77 K)
- Same result for PMOSFET, but different Coulomb scattering coefficient



# LFN model in EKV2.6 and EKV3

in EKV2.6:

$$S_{Id} = \frac{KF G_m^2}{C_{ox} W_{eff} L_{eff} f^{AF}}$$

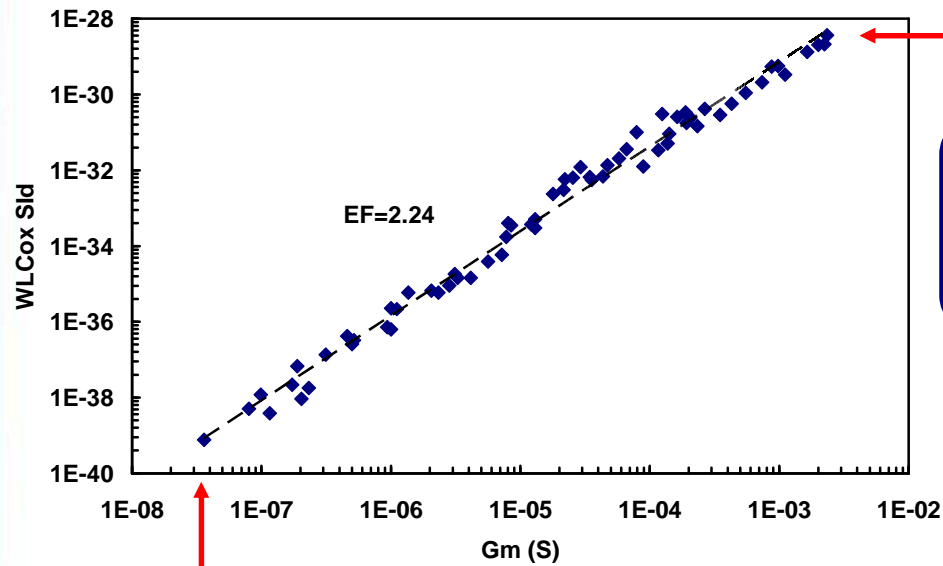
in EKV3:

$$S_{Id} = \frac{KF G_m^{EF}}{C_{ox} W_{eff} L_{eff} f^{AF}}$$

Three parameters: KF, AF, EF ≠ 2

- Only Gm, the gate transconductance
- Simple but efficient model? Valid only in weak inversion?  
Also valid in moderate and strong inversion?

# Test of the EKV3 LFN model at RT

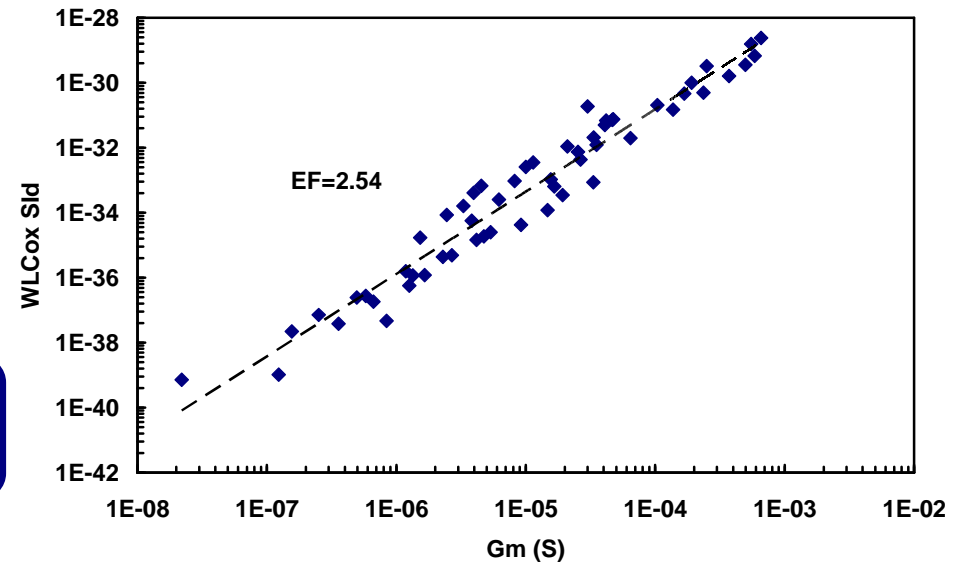


strong inversion

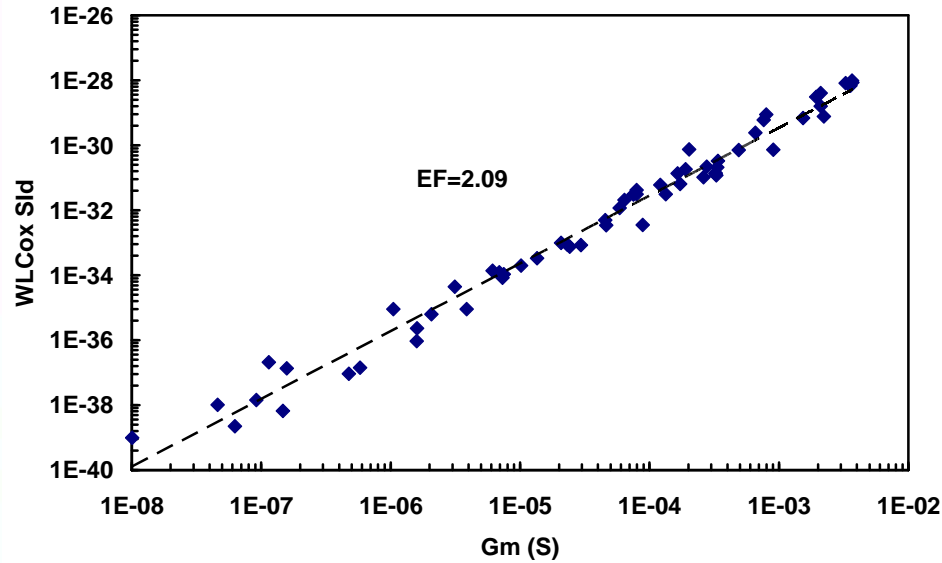
NMOSFET STD 3.3 V P-WELL  
Tox=6.5 nm f=1 Hz

weak inversion

PMOSFET STD 3.3 V N-WELL

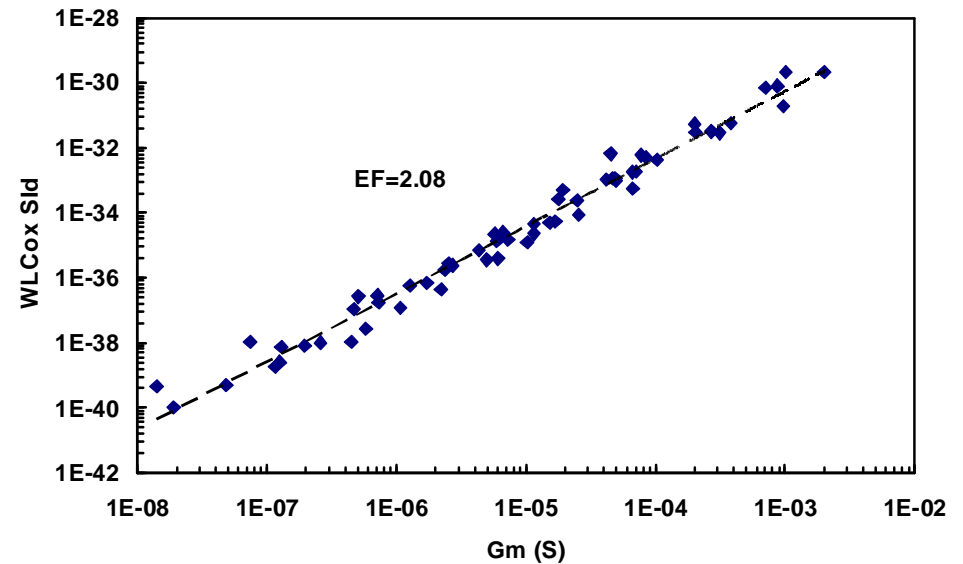


# Test of the EKV3 LFN model at 77 K



**NMOSFET STD 3.3 V P-WELL**

**PMOSFET STD 3.3 V N-WELL**



## Conclusion

- **Measurements of LFN in a 0.18  $\mu\text{m}$  mixed-mode / RF CMOS process at room and low temperature**
- **1/f noise is well described by the  $\Delta N$ - $\Delta\mu$  (improved McWhorter's) model**
- **The Coulomb scattering coefficient is lower at 77 K than at RT**
- **The LF noise model implemented in EKV3 is simple but valid at low temperature in a very wide range of inversion: weak, moderate and strong inversion**
- **Measured EF parameter values are  $\approx 2$  and are device- and technology-dependent**

# Acknowledgements

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