

# Charge Trapping Phenomena in MOSFETs: From Noise to Bias Temperature Instability

**Gilson Wirth**

**UFRGS - Porto Alegre, Brazil**

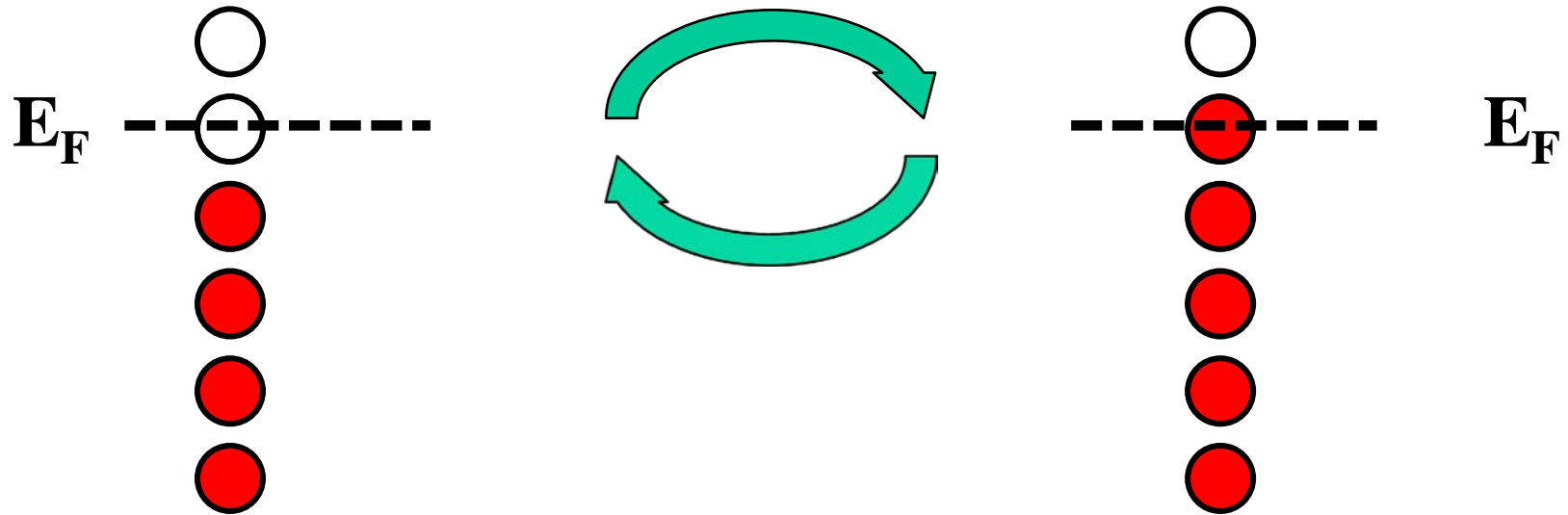


**5th International MOS-AK/GSA Workshop  
San Francisco, California.  
December 12, 2012.**

# Outline

- **Our Modeling Approach for Charge Trapping**
- **Low-Frequency Noise:**
  - **Frequency Domain Models (DC and AC Large Signal)**
  - **Time Domain Analysis and Simulation**
- **NBTI: Charge Trapping Component**
- **Amplitude of the  $\Delta V_T$  Induced by a Trap**
- **Conclusion**

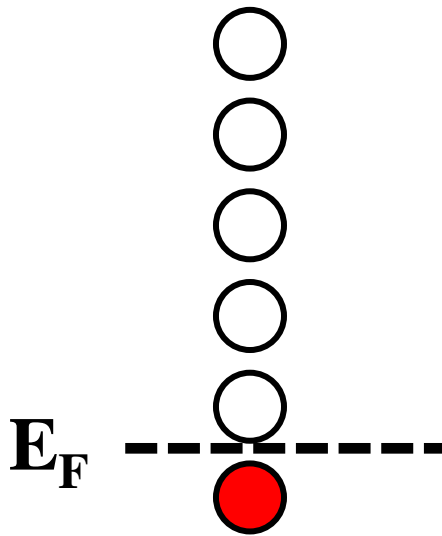
# Low-Frequency Noise



Traps within a few  $k_T$  from the Fermi Level  
contribute to noise

# Charge Trapping Component of BTI

Transistor Off

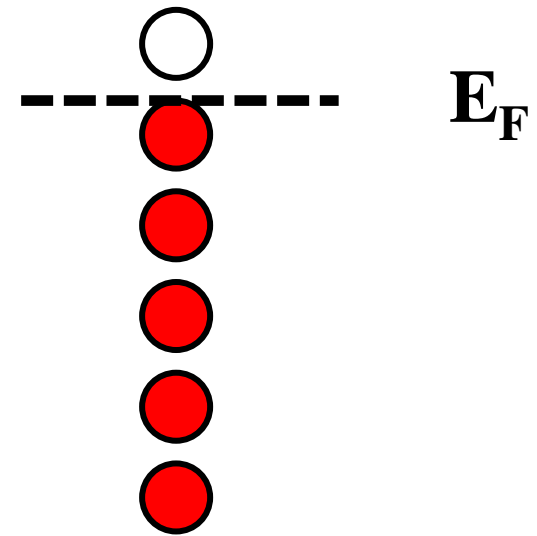


Traps Mostly Empty



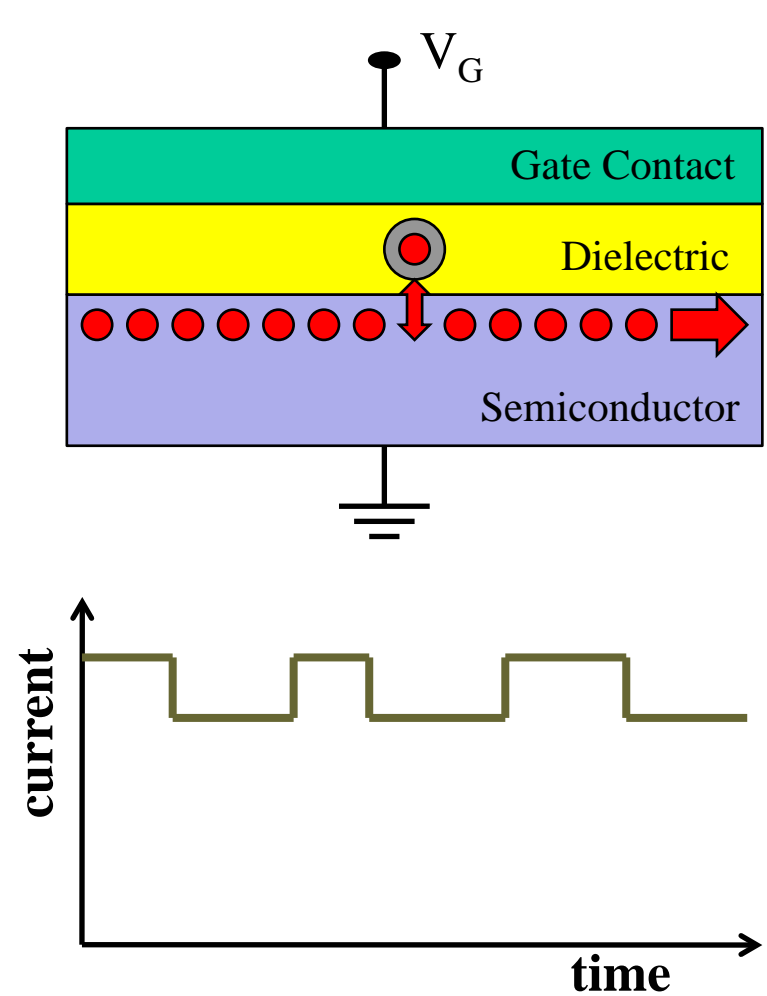
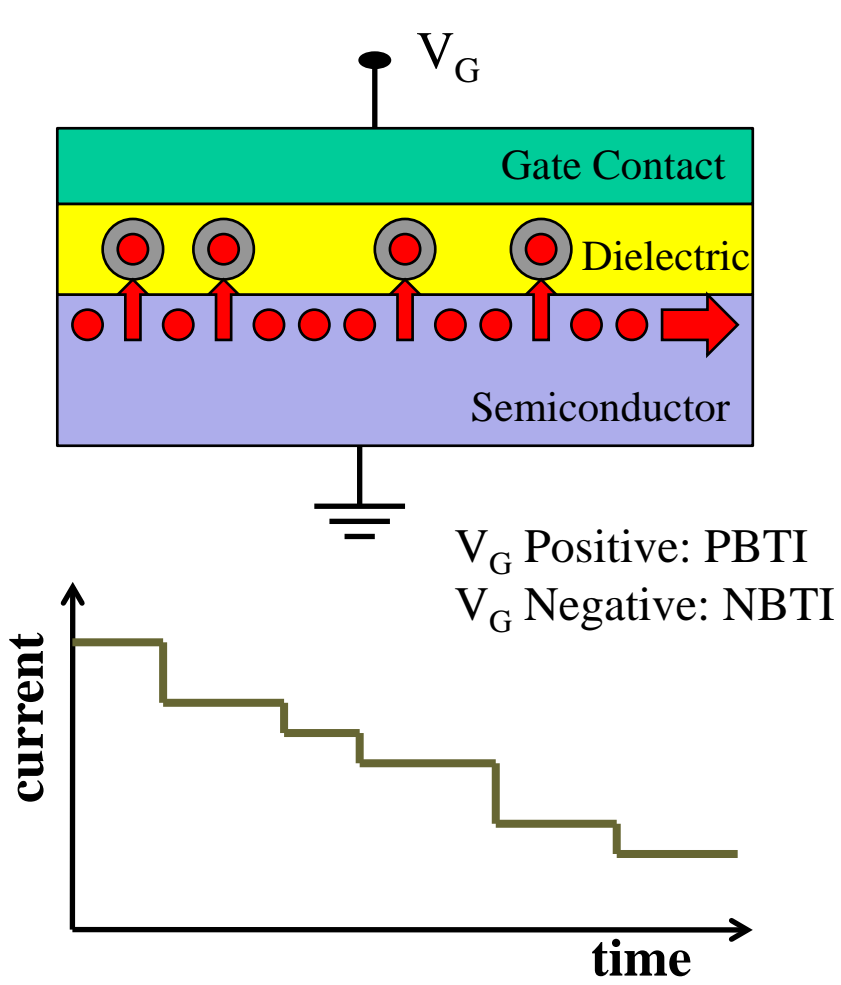
After a  
“Long” Time

Transistor On



Traps Mostly Occupied

# BTI x RTS



# BTI x RTS

Traps that contribute to noise are the ones with

$$\tau_C \cong \tau_E$$

i.e., traps that keep switching state

Traps that contribute to NBTI are the ones with

$$\tau_C < \tau_E$$

i.e, traps that become occupied

# Modeling Approach

Based on **Microscopic (Random) Quantities**, instead of distributed (homogeneous) quantities.

1. Charge trapping and de-trapping are stochastic events governed by characteristic time constants, which are uniformly distributed on a log scale.
2. Number of traps is assumed to be Poisson distributed.
3. Amplitude of the fluctuation induced by a single trap is a random variable, studied by atomistic simulations.
4. Trap energy distribution is assumed to be U shaped (key to explain the AC behavior).

# Some Advantages of our Approach

- 1. Can be Applied to both DC and AC Large Signal Excitation.**
- 2. Can be Applied also for Transient Simulation.**
- 3. Random Variables Lead to Statistical Model (Today Variability is a Major Issue).**
- 4. Can be Applied to Different Phenomena where Charge Trapping Plays a Role, such as Noise and NBTI.**

# Low-Frequency Noise

- **Frequency Domain Modeling (DC)**
  - **Noise due to a Single Trap**
  - **Noise due to the Ensemble of Traps**
- **AC Large Signal Excitation**
  
- **Time Domain (Transient) Analysis and Simulation**

# Evaluating the Noise Power due to **Many** Traps

- Average Value

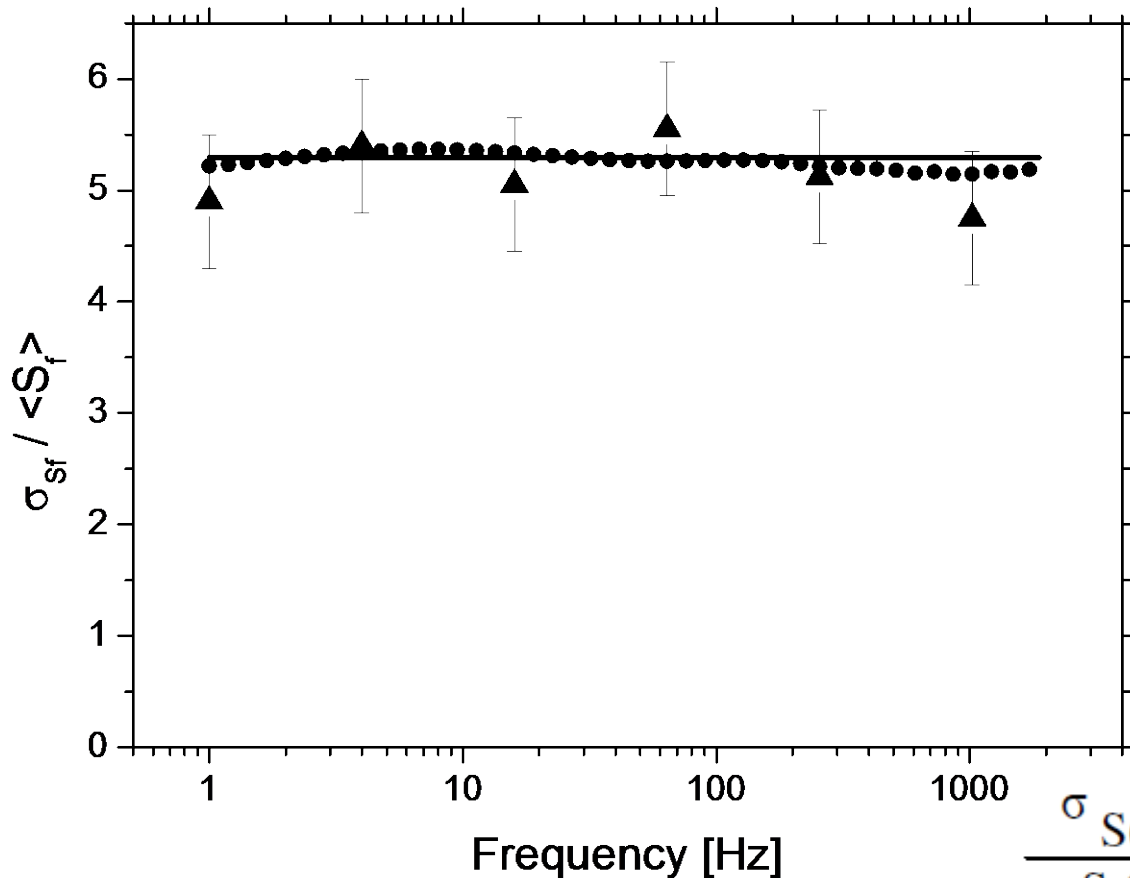
$$\langle S(f) \rangle = \frac{\langle A^2 \rangle N_{\text{dec}} WL}{f} \frac{\pi}{2}$$

- Standard Deviation

$$\frac{\sigma_{S(f)}}{\langle S(f) \rangle} = \frac{\sqrt{2}}{\pi \sqrt{N_{\text{dec}} WL}} \sqrt{\frac{\langle A^4 \rangle}{\langle A^2 \rangle^2}}$$

[G Wirth et al. IEEE Trans Electron Dev, 2005](#)

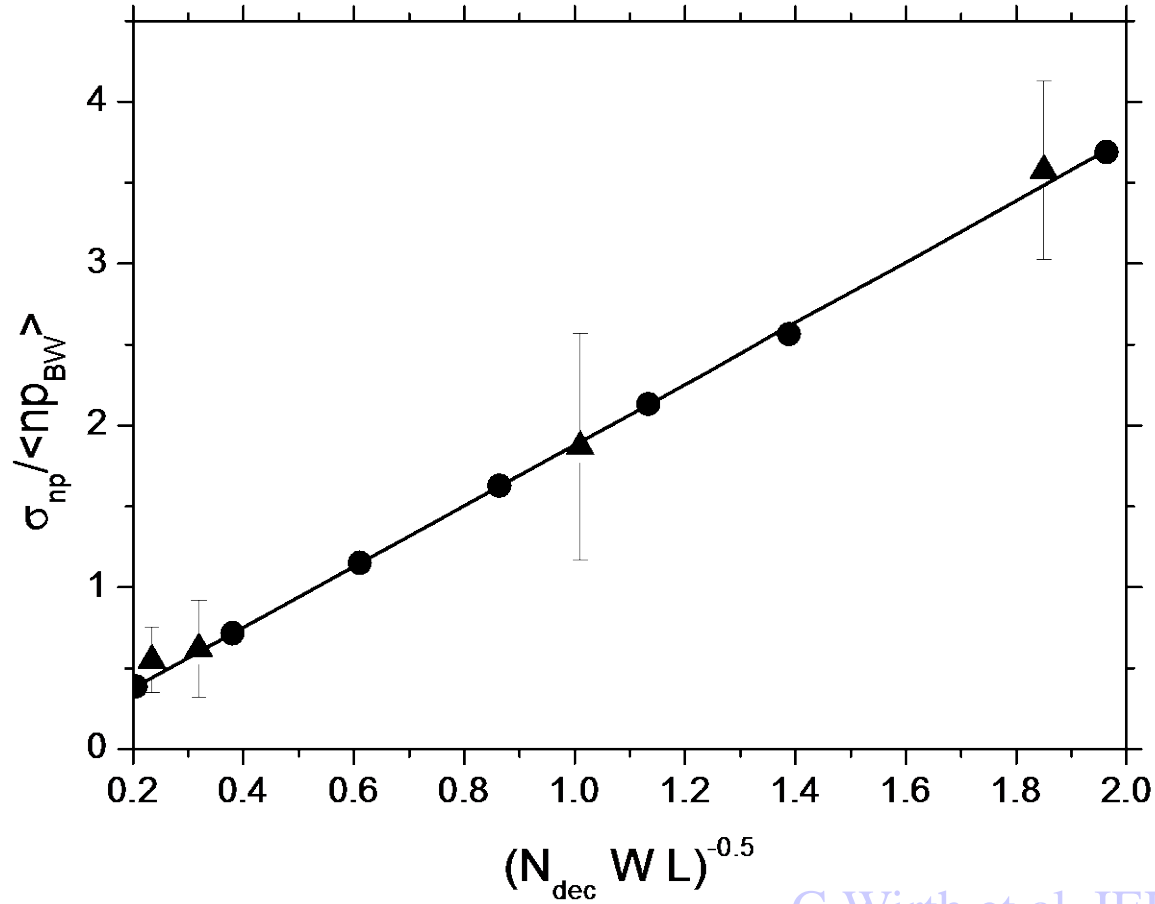
# Variability: Dependency on Frequency



[G Wirth et al. IEEE Trans Electron Dev, 2007](#)

$$\frac{\sigma_{S(f)}}{\langle S(f) \rangle} = \frac{\sqrt{2}}{\pi \sqrt{N_{\text{dec}} WL}} \sqrt{\frac{\langle A^4 \rangle}{\langle A^2 \rangle^2}}$$

# Variability Scaling



**Triangles: Measurement**  
**Dots: Monte Carlo Simulation**  
**Line: Model**

[G Wirth et al. IEEE Trans Electron Dev, 2005](#)

# Low-Frequency Noise

---

- Frequency Domain Modeling (DC)
  - Noise due to a Single Trap
  - Noise due to the Ensemble of Traps
- **AC Large Signal Excitation**
- Time Domain (Transient) Analysis and Simulation

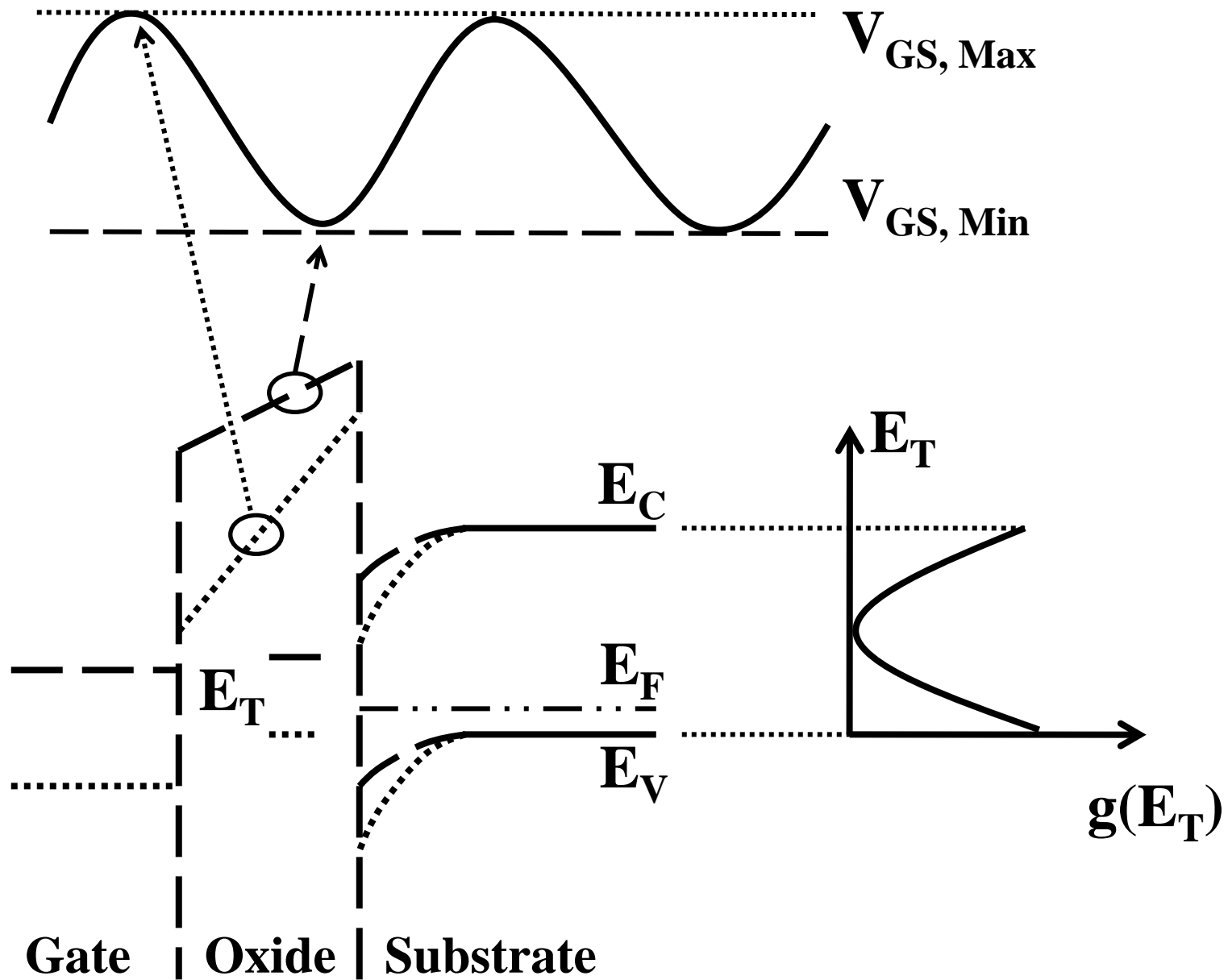
# Switched Bias: Modulation Theory

we can expect for 50% duty cycle, as the switching operation can be represented as multiplication of the  $1/f$  noise current with a square-wave signal with 50% duty cycle,  $m(t)$ , as follows:

$$m(t) = \frac{1}{2} + \frac{2}{\pi} \sin \omega_{sw} t + \frac{2}{3\pi} \sin 3\omega_{sw} t + \frac{2}{5\pi} \sin 5\omega_{sw} t + \dots \quad (1)$$

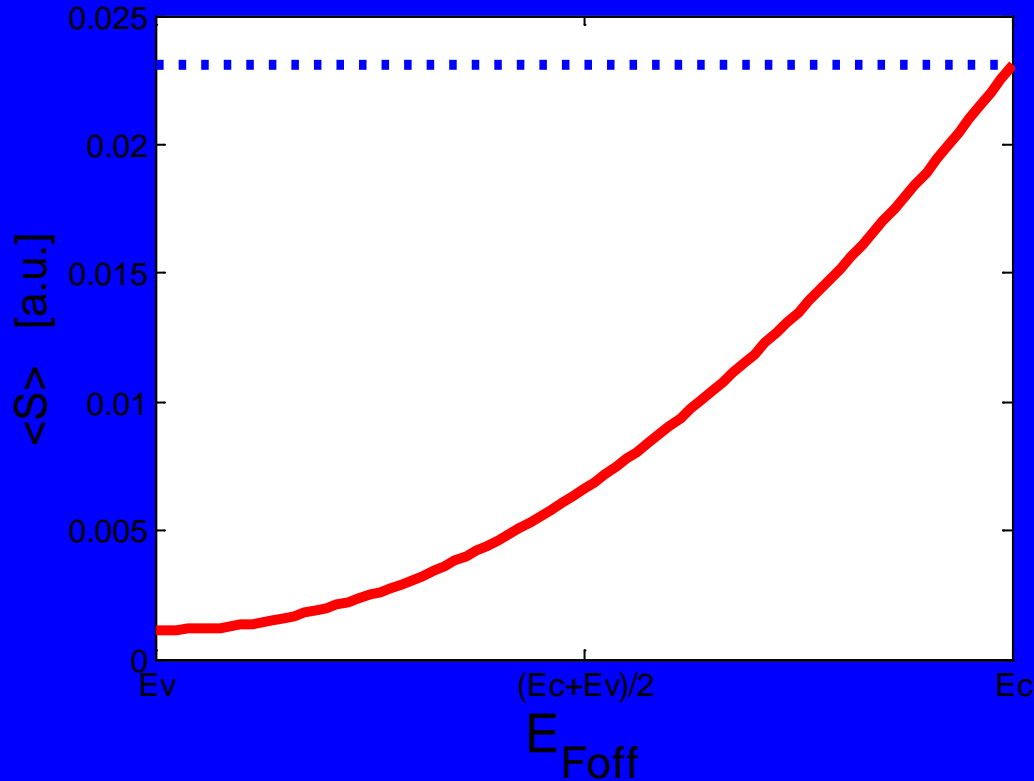
In the frequency domain this corresponds to a convolution of the PSD of the  $1/f$  noise with a spectrum with delta functions at dc,  $\omega_{sw}$ ,  $3\omega_{sw}$ ,  $5\omega_{sw}$ , etc. The dc-term determines the resulting noise power in baseband, which is  $(1/2)^2$  (or  $-6$  dB) compared to the original  $1/f$  noise power.

Klumperink et al., IEEE J. SOLID-STATE CIRC, VOL. 35, NO. 7, 2000



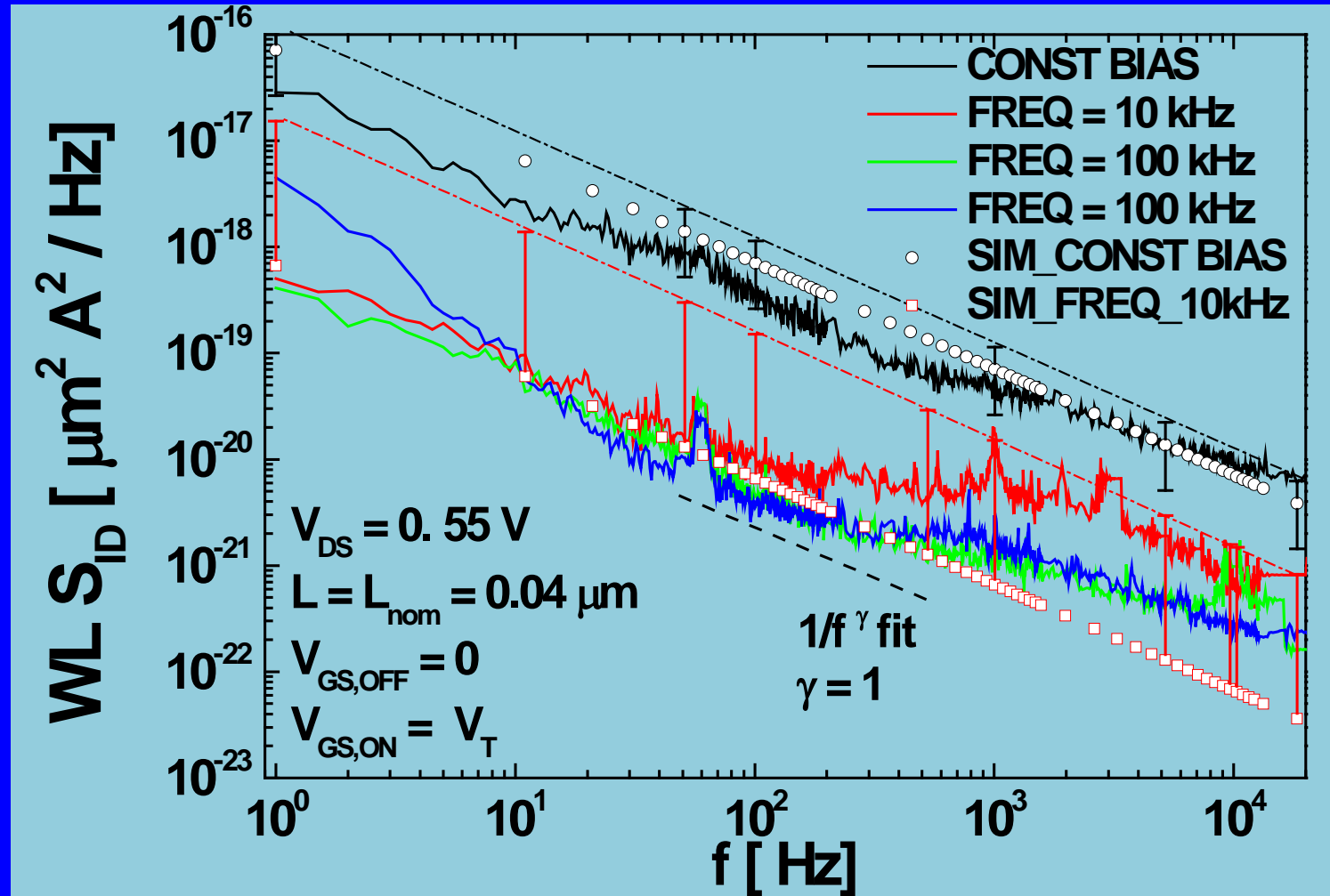
# Switched Bias: Noise Mean Value Decreases

Noise power as a function of the Fermi level in the off phase



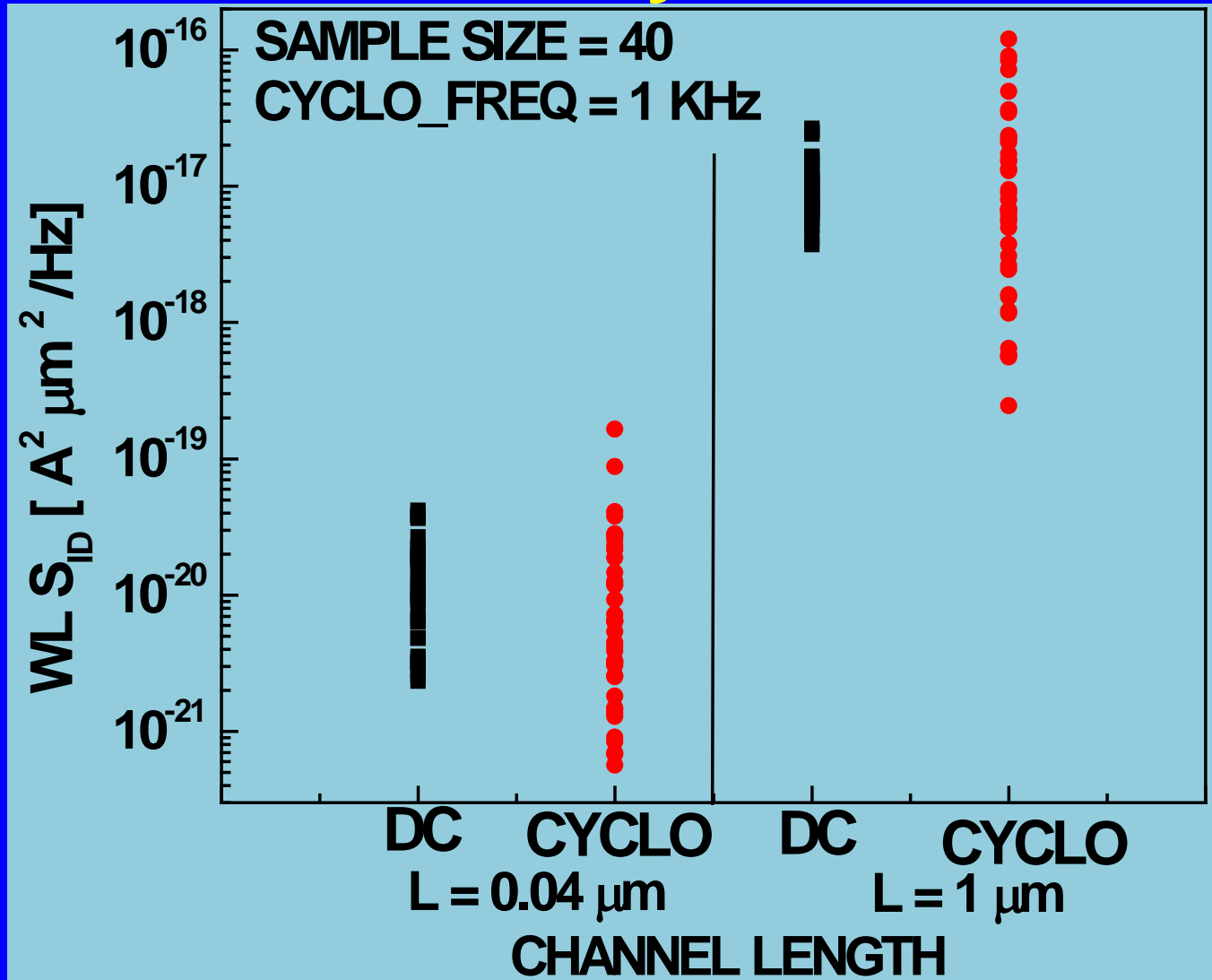
Noise power as a function of the Fermi level in the off phase. In the on phase of the device, the Fermi level is assumed to be fixed, close to the conduction band. The blue dotted line shows the behavior as predicted by standard models used today (e.g. BSIM). The red solid line shows the behavior as predicted by the model here presented.

# Noise Reduction under Cyclo-Operation



- Modulation theory predicts four times noise reduction for CS operation
- Noise reduction is larger and in good agreement to the proposed model.

# Normalized Variability of Noise Behavior



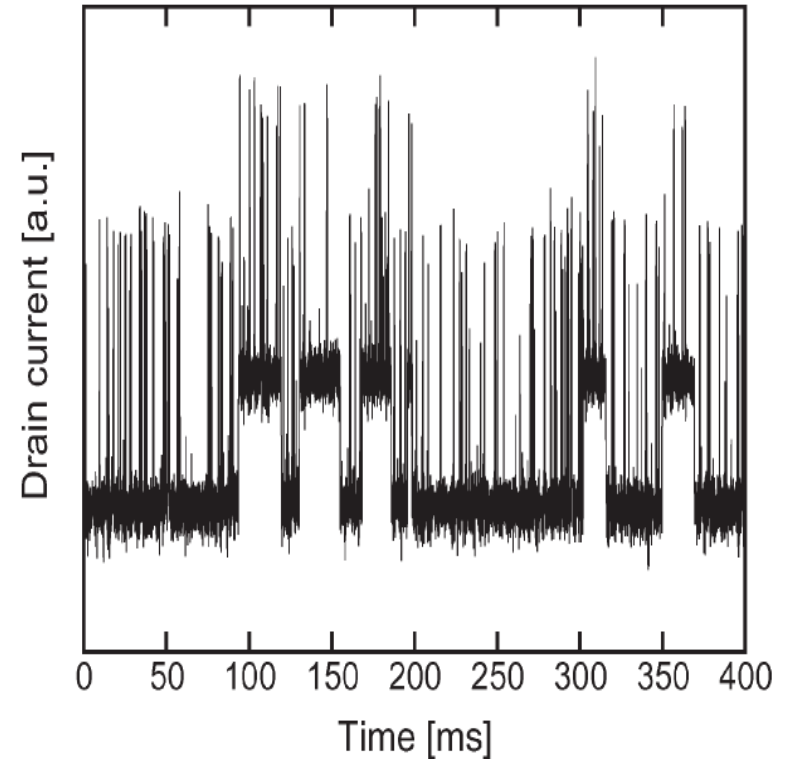
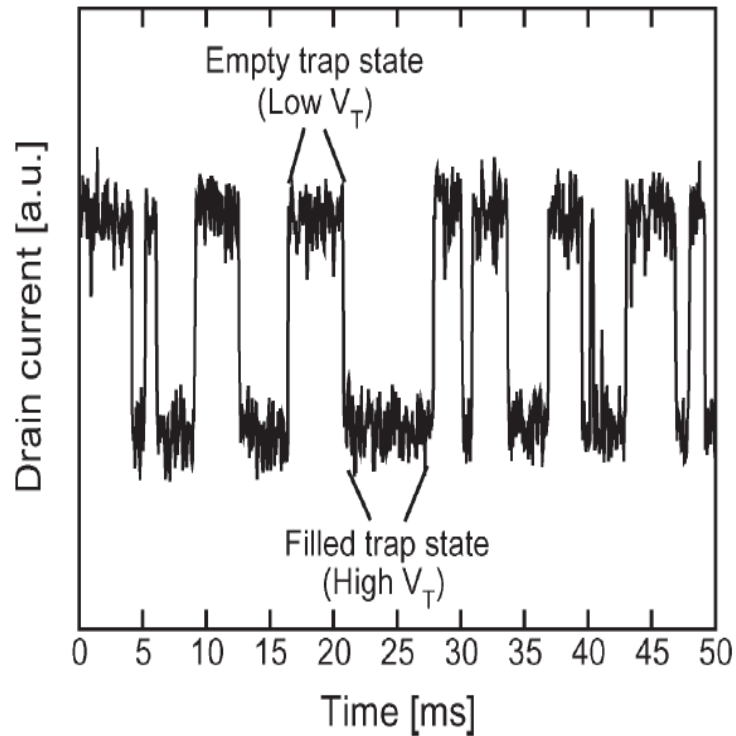
Variability is seen to increase under Cyclo-Stationary Operation.

# Low-Frequency Noise

---

- Frequency Domain Modeling (DC)
  - Noise due to a Single Trap
  - Noise due to the Ensemble of Traps
- AC Large Signal Excitation
- **Time Domain (Transient) Analysis and Simulation**

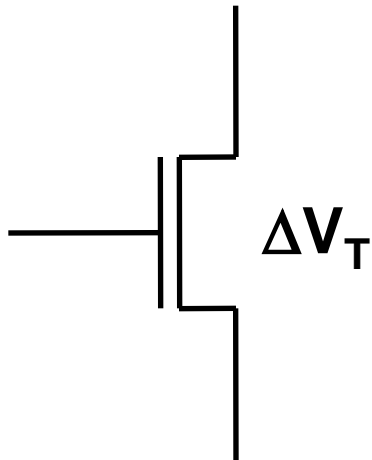
# RTS and Time Domain



## $V_T$ Fluctuations

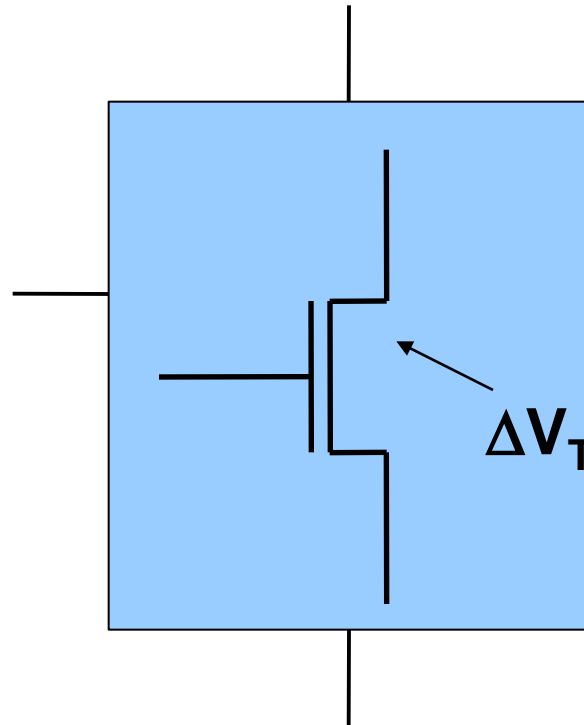
# Possible Simulation Methodologies

Static

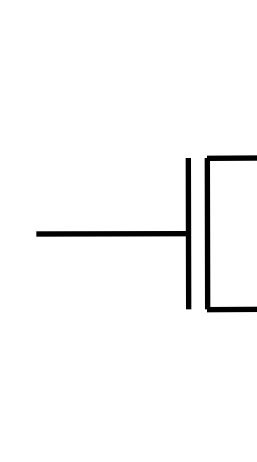


Change  $dV_t$  at instantiation

Dynamic



Verilog-A wrapper to Trans. model



$$I_{ds} = \dots + f(\text{delvto}(t))$$

Change transistor Model equations

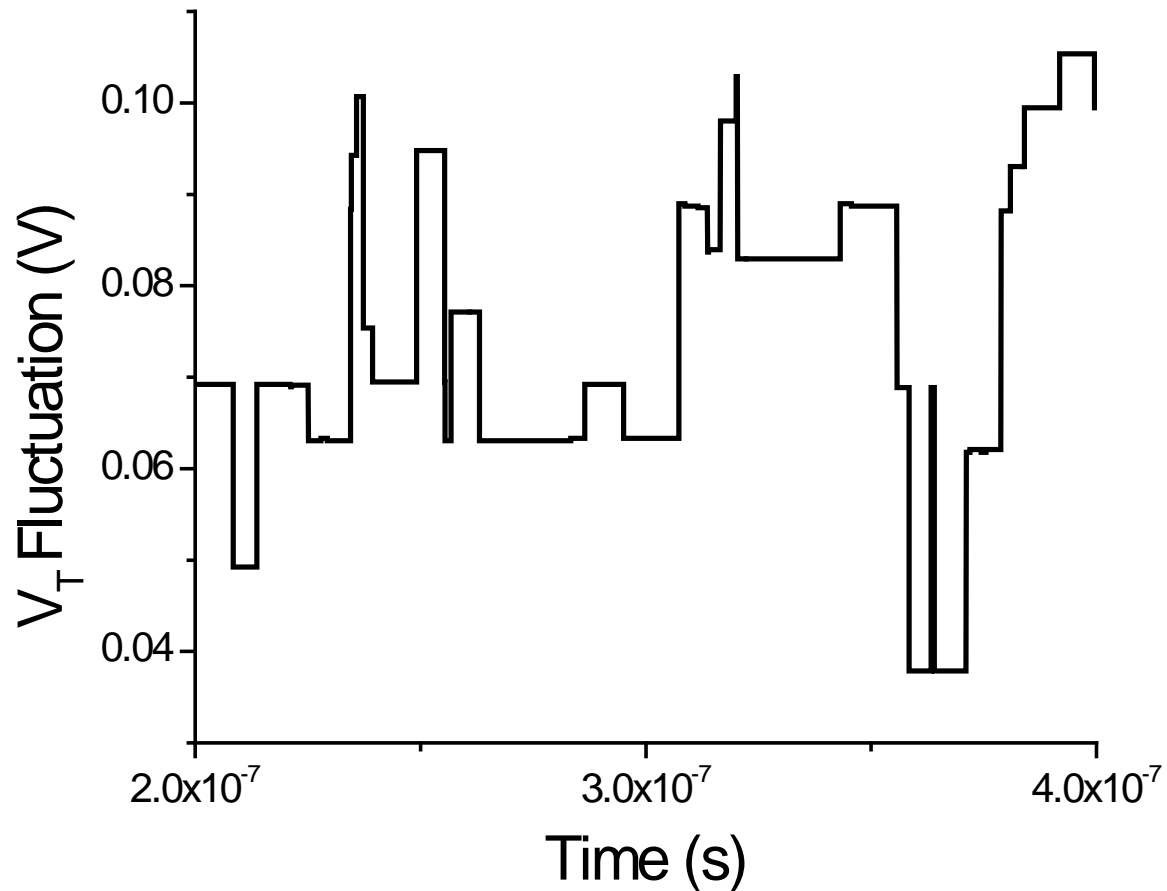
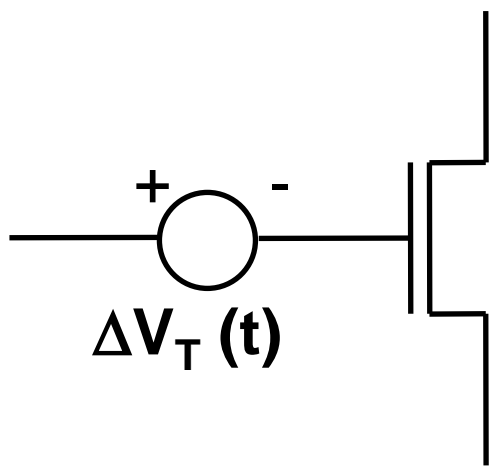
# RTS: Transient Simulation (1)

- Charge trapping and de-trapping are stochastic events, governed by capture and emission time constants,  $\tau_c$  and  $\tau_e$ , which are uniformly distributed on a log-scale;
- the number of traps ( $N_{tr}$ ) is assumed to be Poisson distributed, and the average number of traps (parameter of the Poisson) is assumed to be proportional to the channel area;
- trap energy distribution,  $g(E_T)$ , is assumed to be U-shaped;
- the amplitude of the  $V_T$  fluctuation induced by a single trap, is a random variable given by atomistic device simulations.

## RTS: Transient Simulation (2)

- At each simulation time step, it is checked if a trap changes state.
- Trap switching probability is evaluated based on the device bias point at each transient simulation step.
- If one or more trap change state, transistor threshold voltage is changed accordingly.
- **Simulators do not support this kind of simulation:**
  - ngspice and BSIM4 code modified.

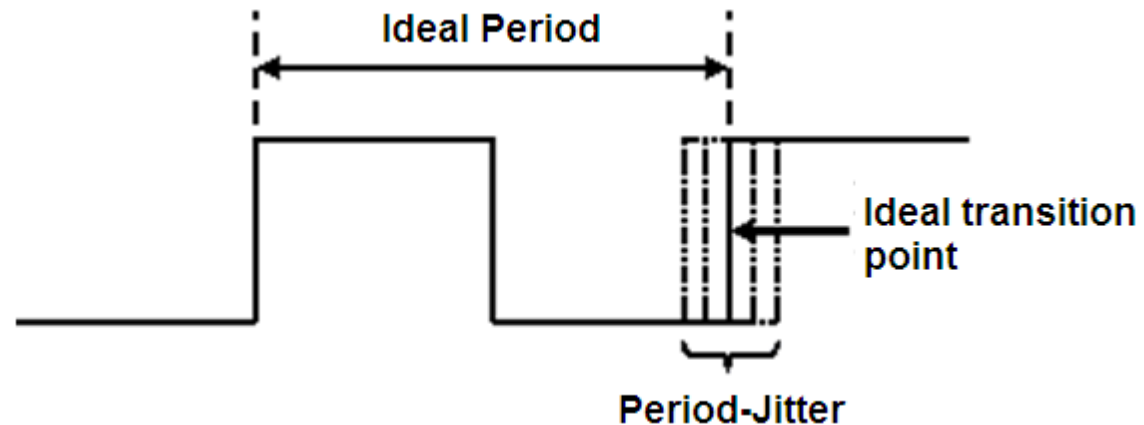
# $V_T$ Fluctuates Over Time



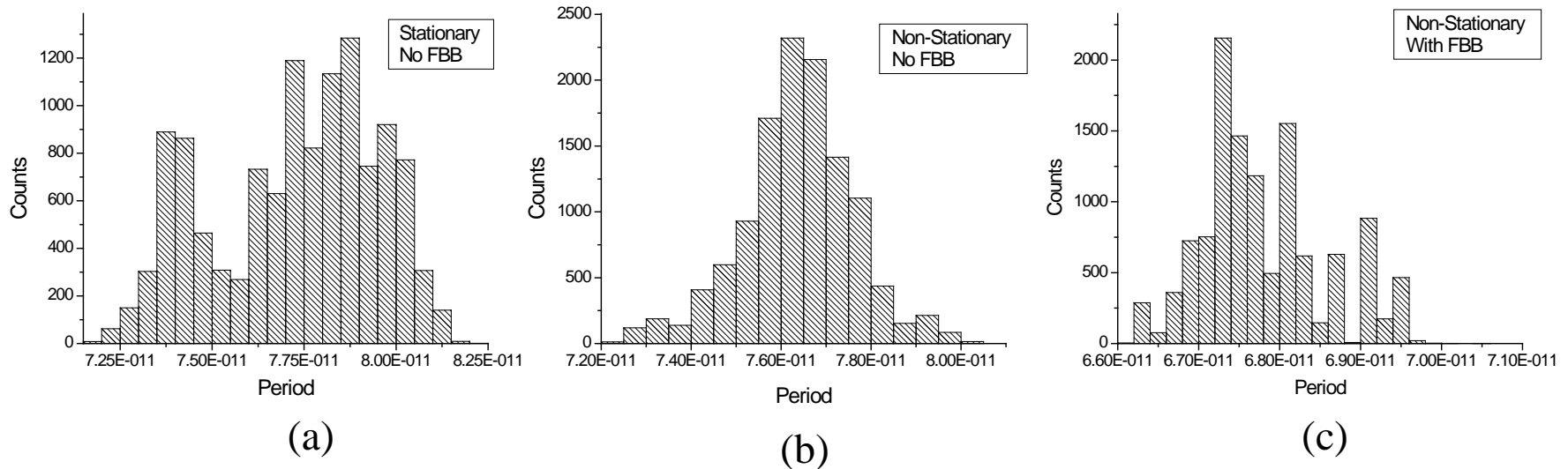
# Ring Osc Period Jitter

- **Period Jitter**

- Period Jitter is the difference between a clock period and the ideal clock period (it can occur after or before the ideal transition).



# Transient Simulation of a Ring Oscillator



**Histogram of oscillation period:**

**(a) stationary DC noise analysis,**

**(b) and (c) non-stationary simulation methodology here proposed.**

**Case (c) is for the oscillator under forward body biasing (FBB).**

**Stationary noise analysis predicts a jitter ( $\sigma_T$ ) of 2.2ps, non stationary analysis predicts a 1.3ps jitter. FBB decreases  $\sigma_T$  to 0.8ps.**

# Comments

---

- **Pros**

- Properly implements the physical-based equations into a circuit simulator
- Computationally efficient (minor impact on the run time of the transient simulation)
- Easy to use: Transparent for the circuit designer (no change needed in the netlist).
- Monte Carlo “by its nature”.

- **Cons**

- Changes made on simulator source code: time intensive work, and restriction to access proprietary code (HSpice, Spectre, etc.)

# Outline

---

- **Our Modeling Approach for Charge Trapping**
- **Low-Frequency Noise:**
  - **Frequency Domain Models (DC and AC Large Signal)**
  - **Time Domain Analysis and Simulation**
- **NBTI: Charge Trapping Component**
- **Amplitude of the  $\Delta V_T$  Induced by a Trap**
- **Conclusion**

# NBTI: Charge Trapping Component

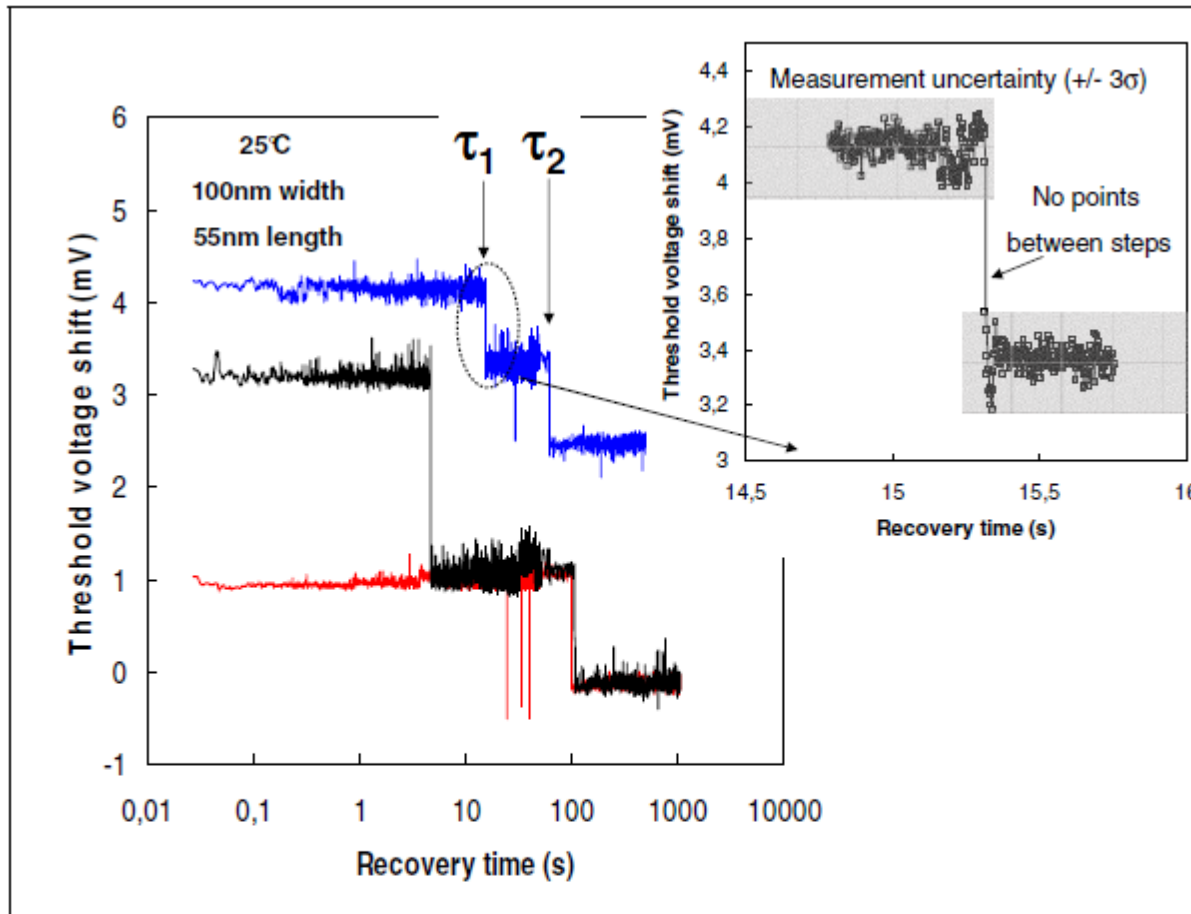
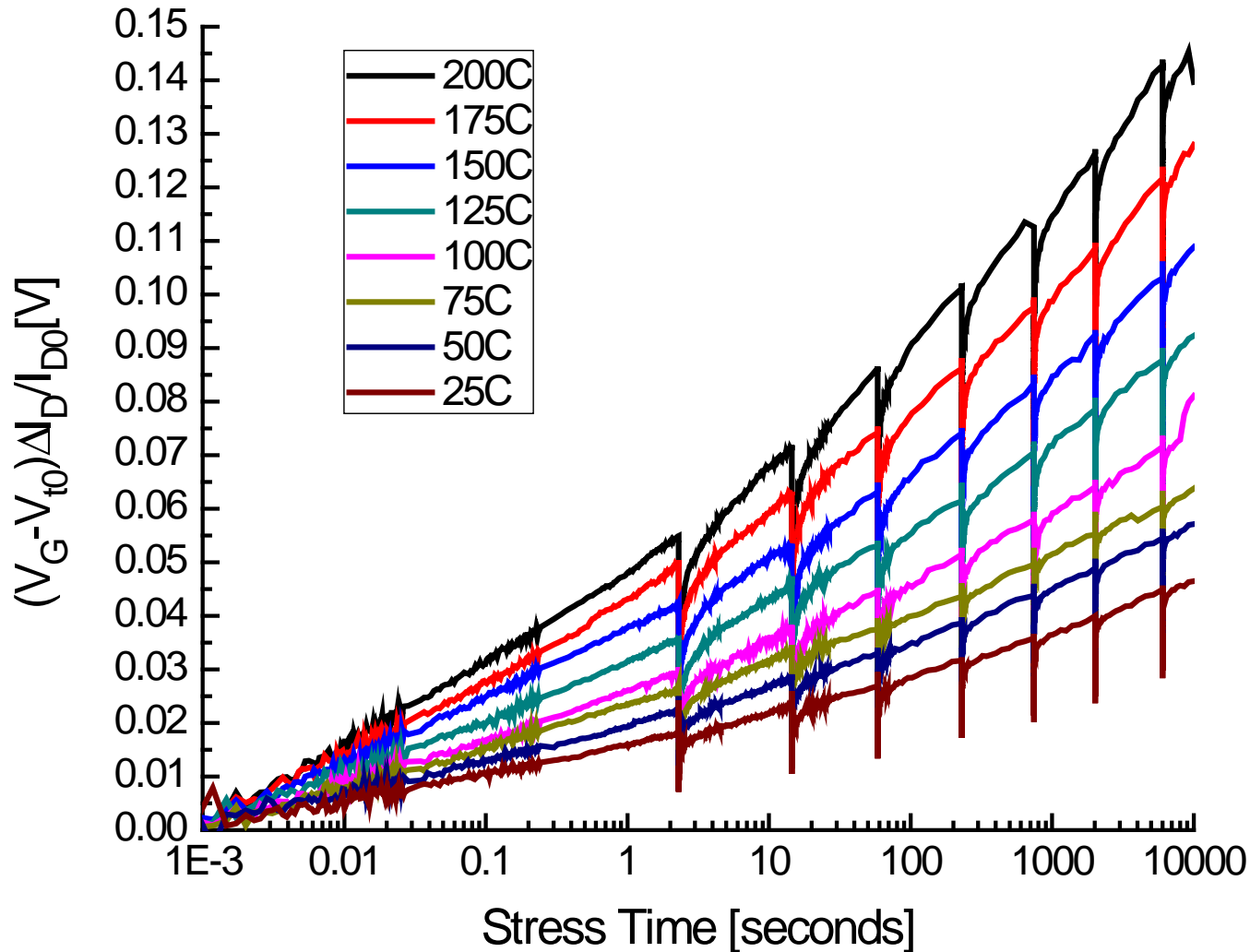


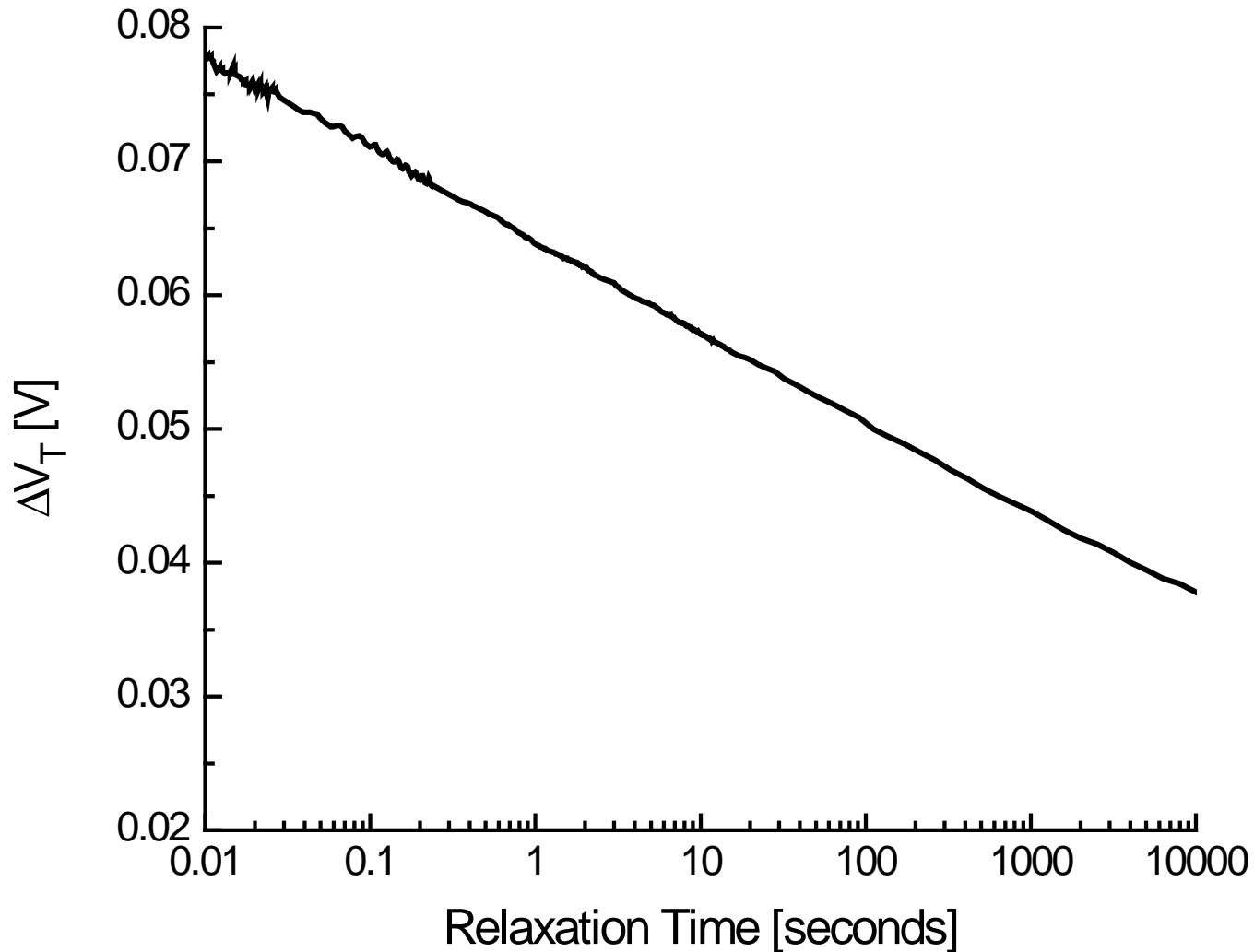
Figure 7: Recovery of  $V_{TP}$  shifts for several SRAM-sized devices showing the discrete nature of detrapping events. The inset shows that there are no intermediary values between steps in spite of the small measurement step time (shaded area represents the measurement uncertainty  $(\pm 3\sigma)$ ).

Huard et al.,  
IRPS 2008

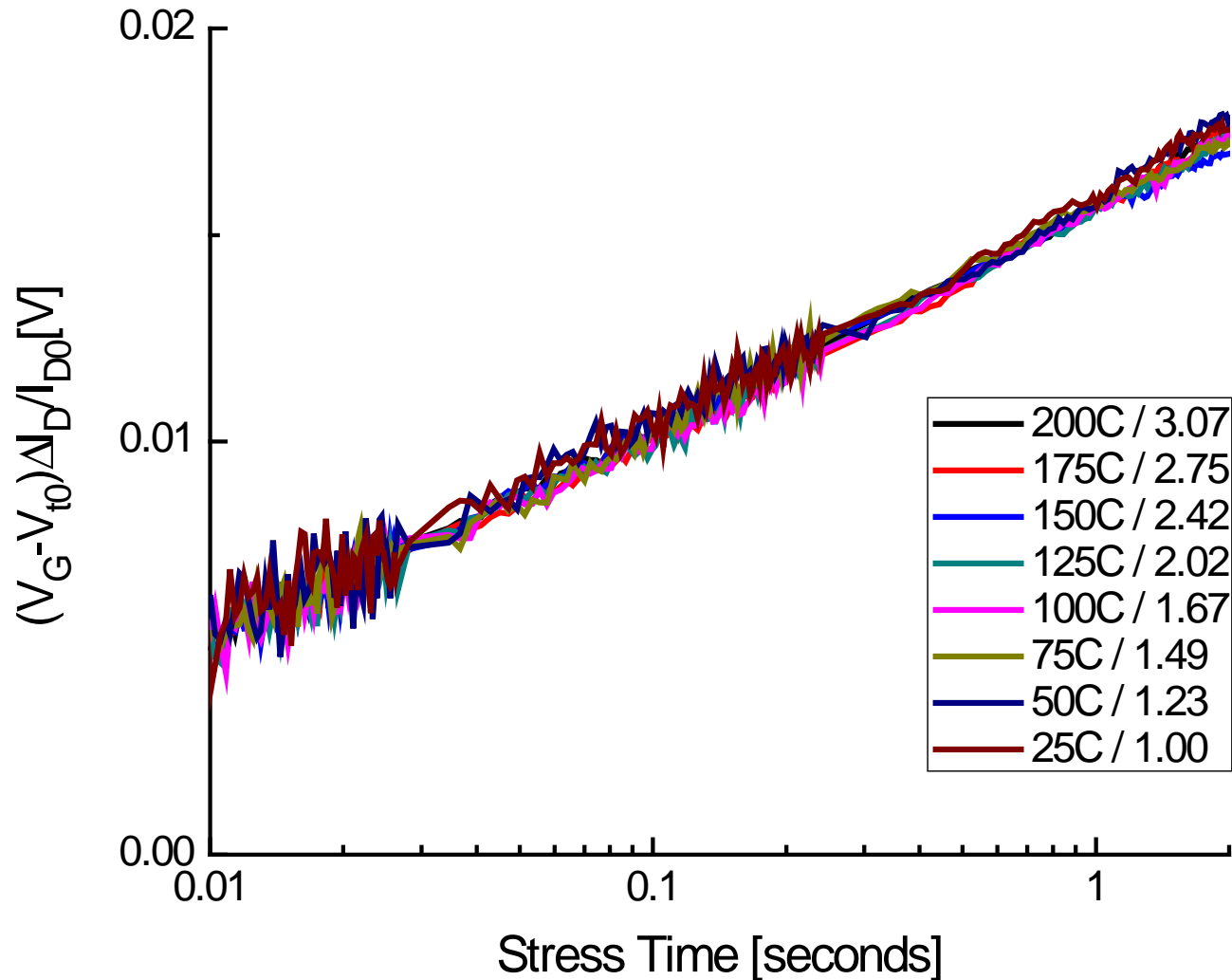
# NBTI: Stress Phase



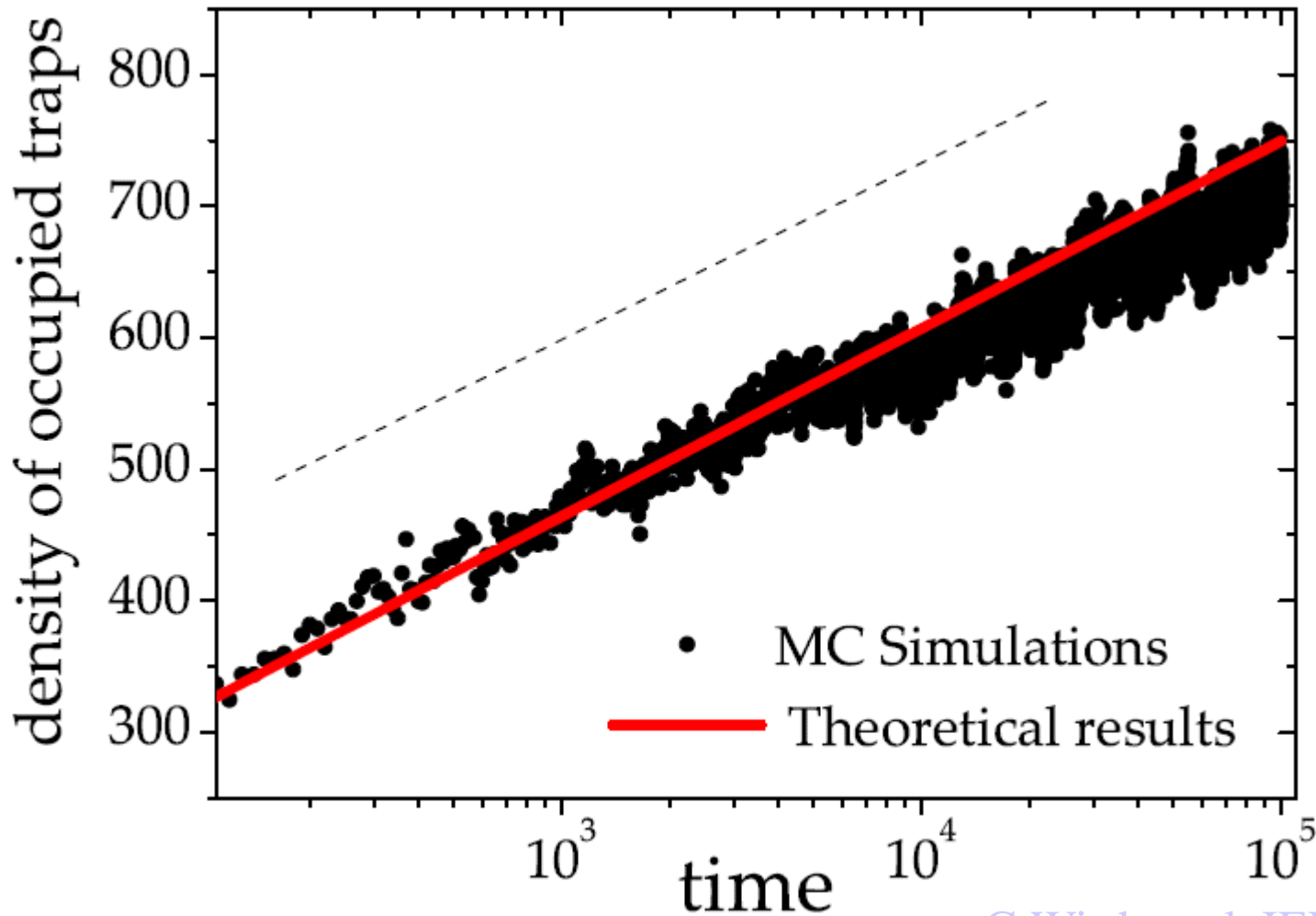
# NBTI: Relaxation Phase



# NBTI: Temperature Dependence



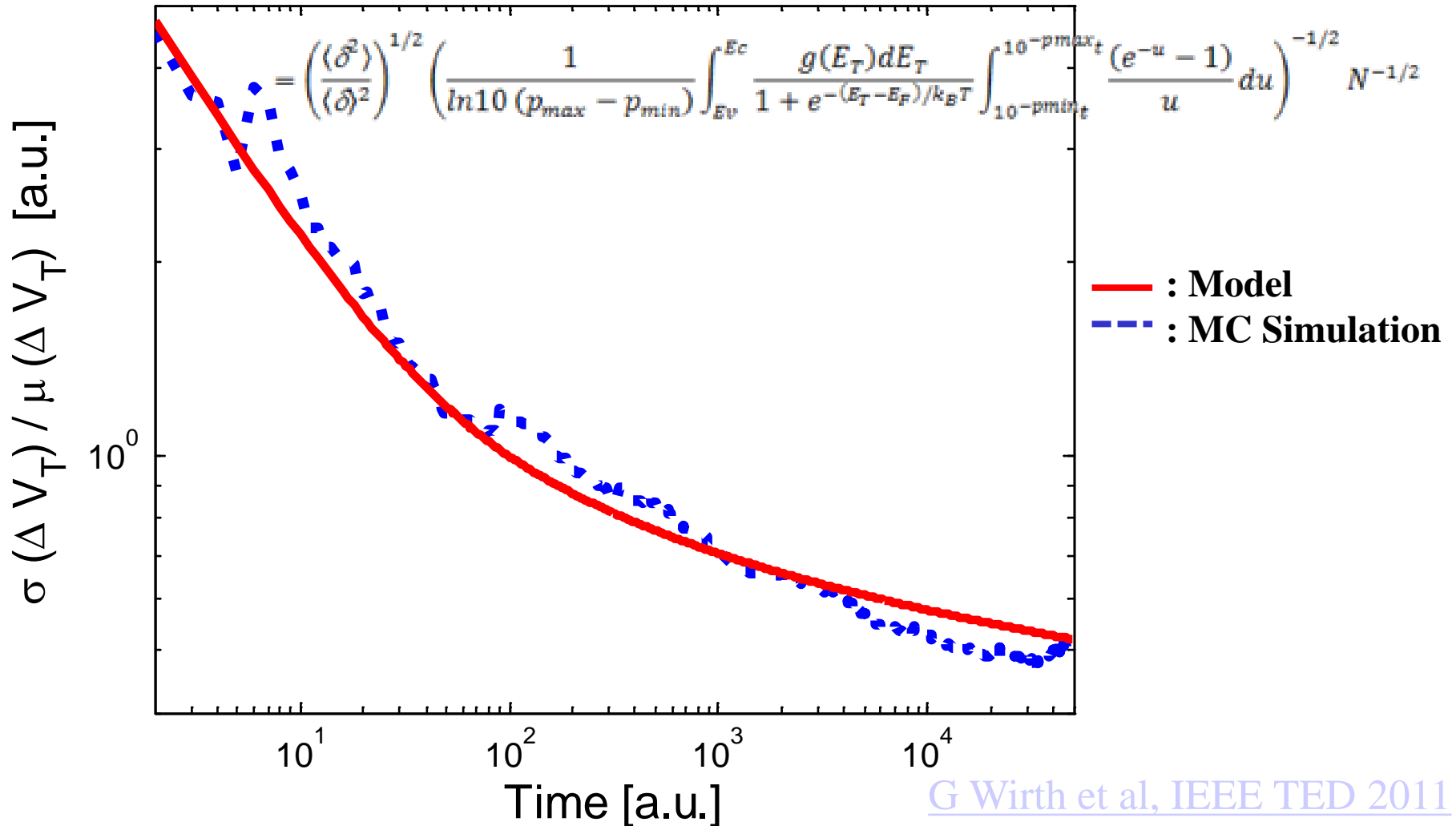
# Model for the Charge Trapping Component



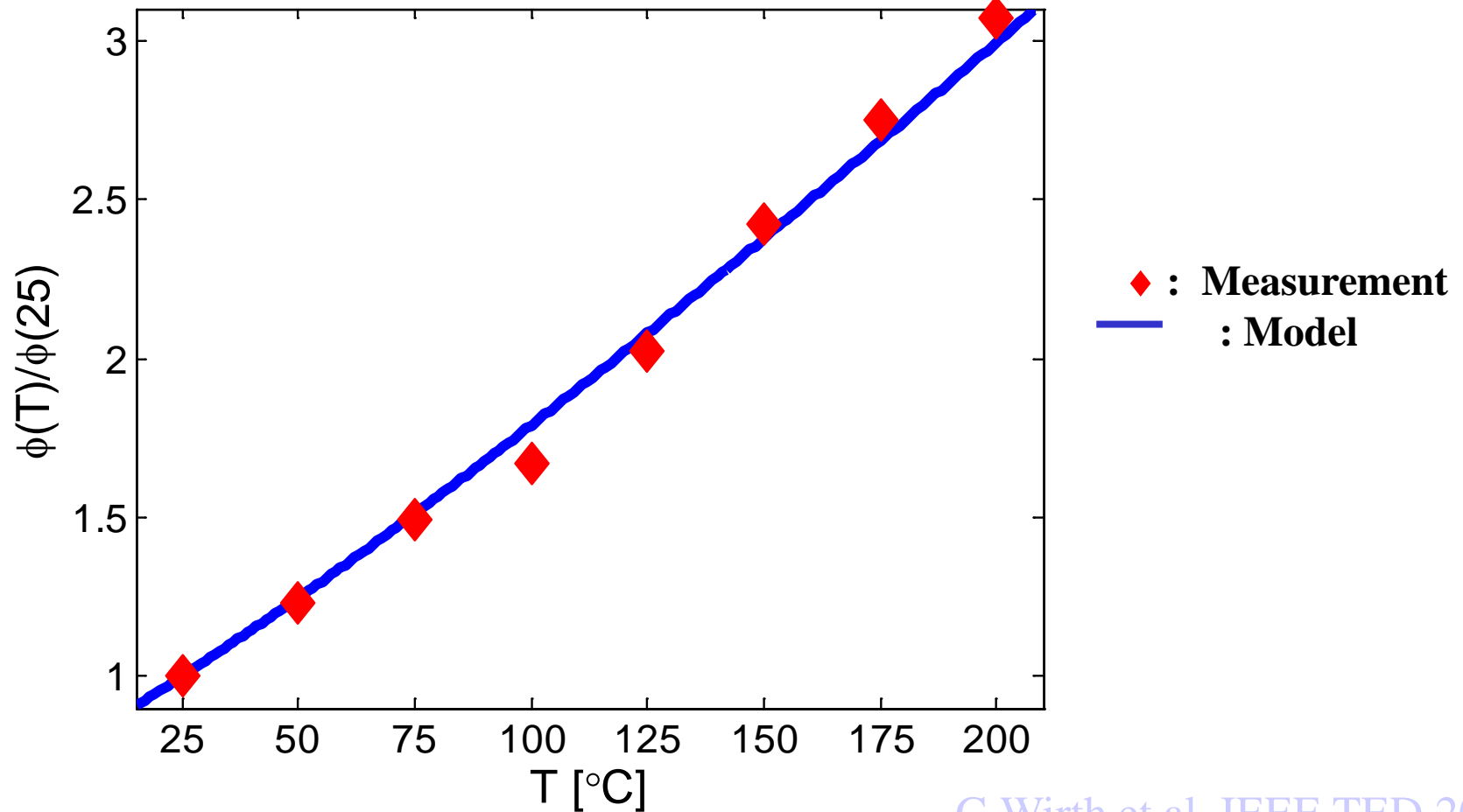
[G Wirth et al, IEEE TED 2011](#)

$$\overline{\langle n(t) \rangle} \sim \varphi(T, E_F)(A + B \log t)$$

# Normalized standard deviation of the BTI induced $V_T$ shift

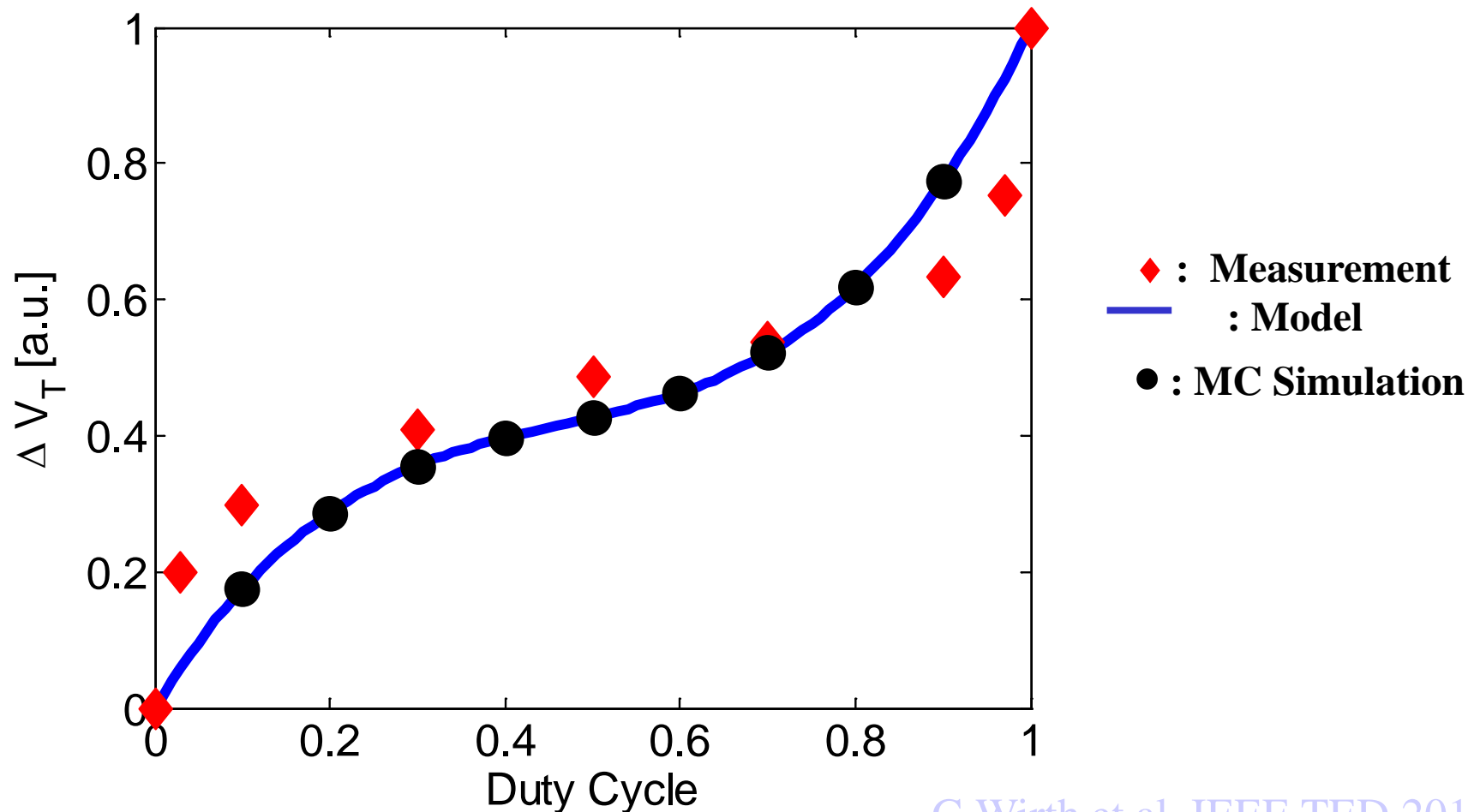


# Temperature Dependence



[G Wirth et al, IEEE TED 2011](#)

# Circuit Activity (Duty Cycle) Dependence

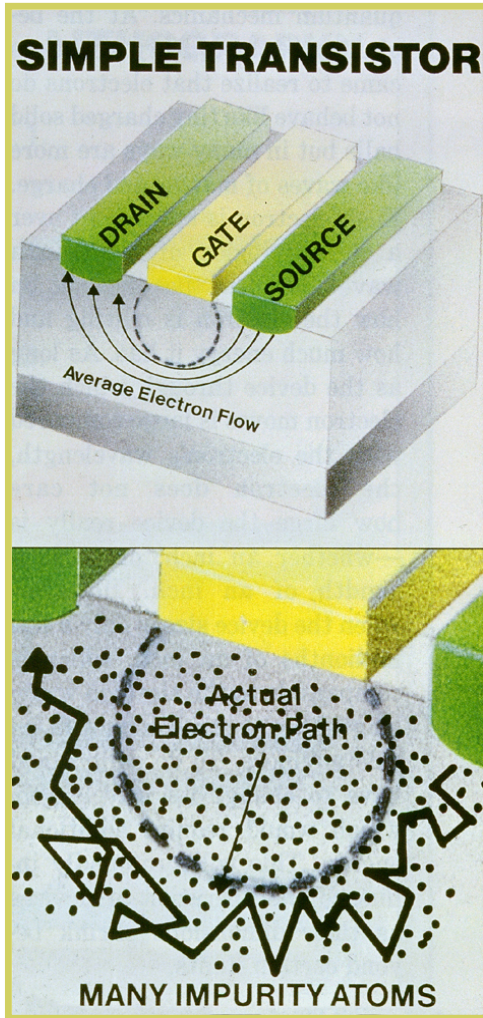


[G Wirth et al, IEEE TED 2011](#)

# Outline

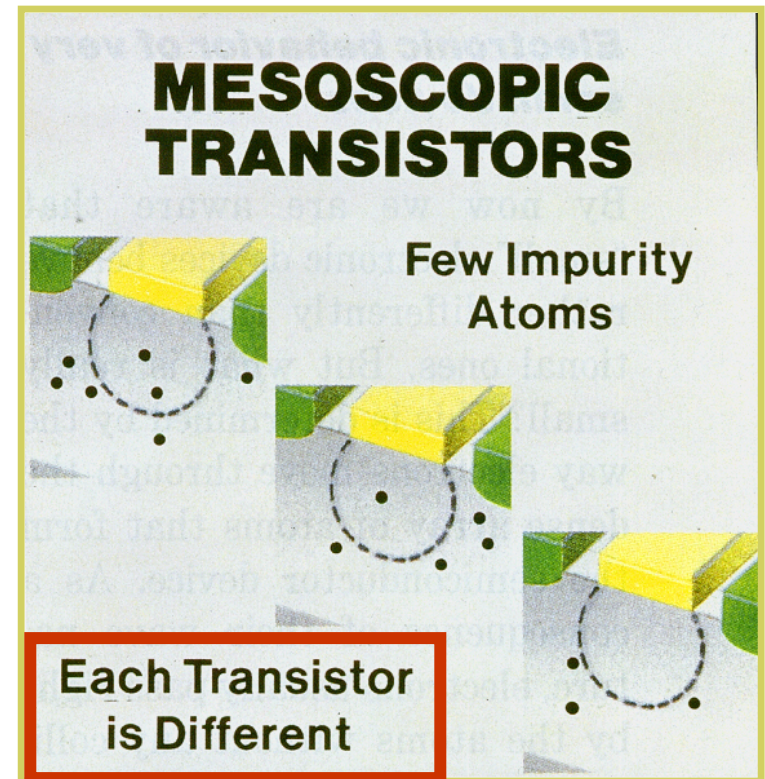
- Our Modeling Approach for Charge Trapping
- Low-Frequency Noise:
  - Frequency Domain Models (DC and AC Large Signal)
  - Time Domain Analysis and Simulation
- NBTI: Charge Trapping Component
- **Amplitude of the  $\Delta V_T$  Induced by a Trap**
- Conclusion

# RDF: Random Dopant Fluctuations



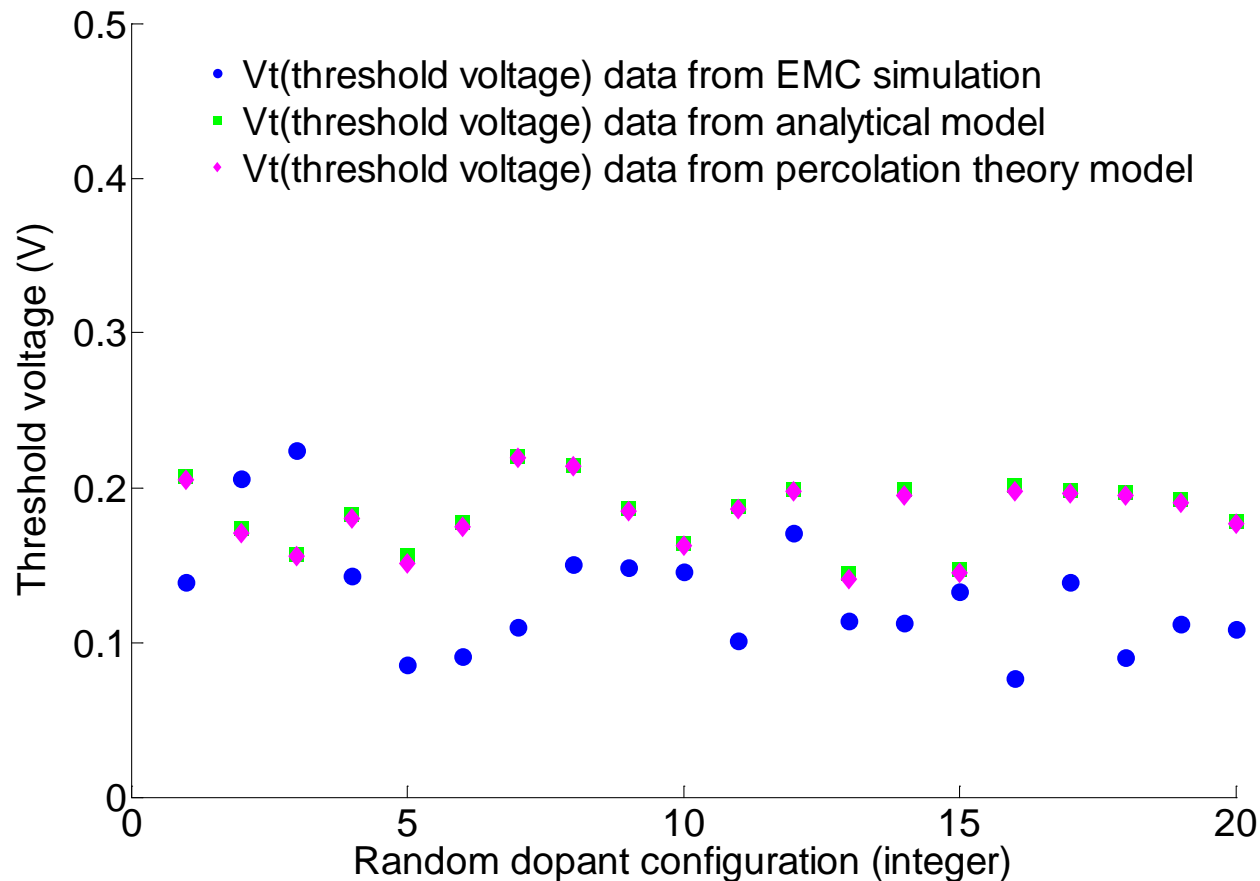
In the **past** all transistors were similar because of *self averaging*

**Today**, Each Transistor is Different



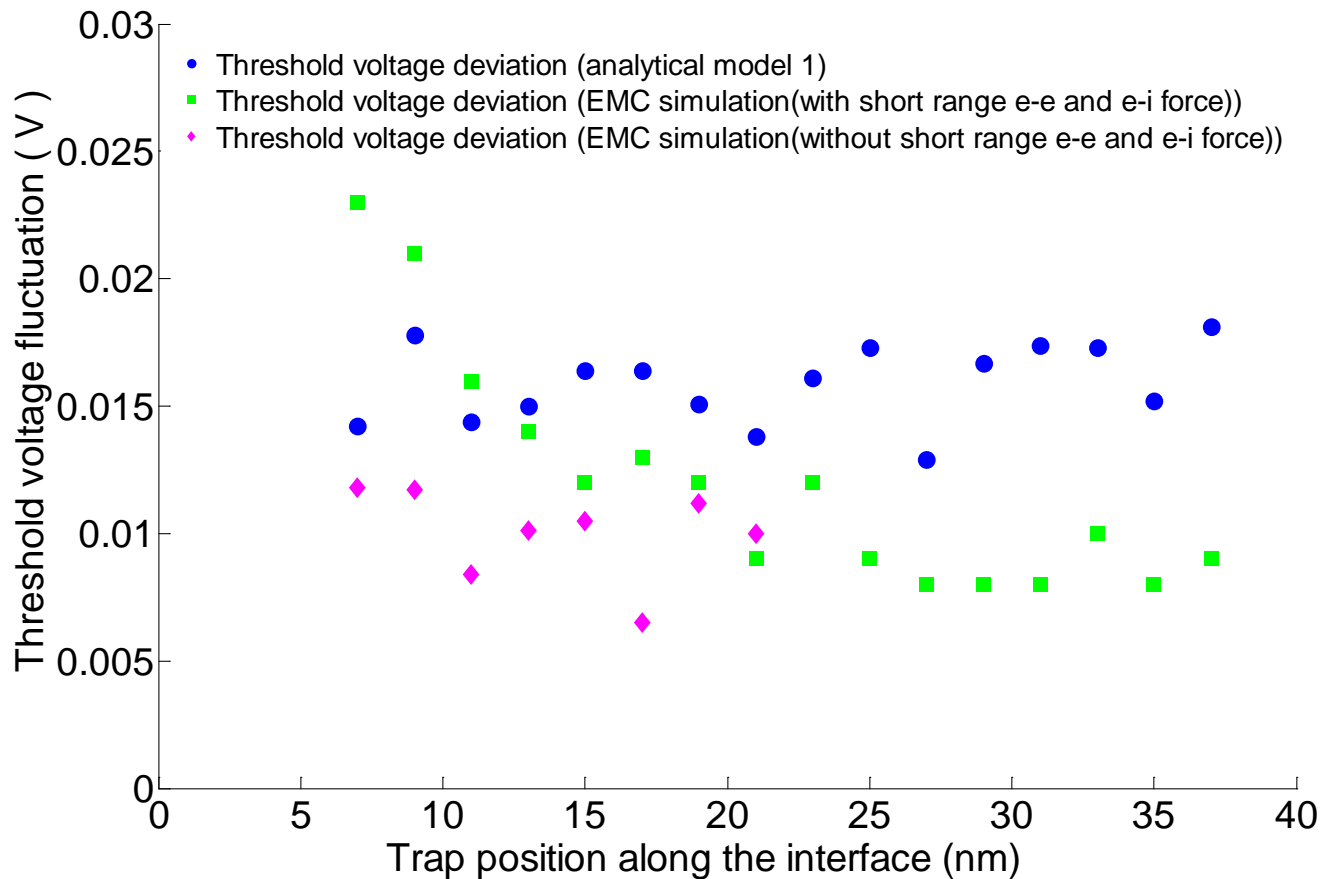
Slide Courtesy Prof Dragica Vasileska, ASU

# Threshold Voltage Values For Different RDF Configurations



[N Ashraf et al, IEEE EDL 2011](#)

# Dependence of $V_T$ Fluctuations on Trap Position Along the Channel



[N Ashraf et al, IEEE EDL 2011](#)

# Conclusion

A microscopic, statistical modeling approach for charge trapping is presented.

It is applied to study the role of charge trapping and de-trapping in Noise and BTI.

Mutual relation between different reliability phenomena (LF noise, BTI and RDF) is discussed.

The modeling approach may be applied for time domain (transient) or frequency domain analysis.

# Work here presented is due to

- People at UFRGS, Brazil: Roberto da Silva, Lucas Brusamarello, Vinicius Camargo, Mauricio Silva, Gilson Wirth, and many others ...
- People at ASU, USA: Dragica Vasileska and Nabil Ashraf.
- People at Texas Instruments: Ralf Brederlow and P Srinivasan (SP).
- People at IMEC, Belgium: Ben Kaczer, Philippe Roussel, Guido Groeseneken, Maria Toledano-Luque, Jacopo Franco, ...
- and many others ...